

# Investigation of CR heliospheric propagation models during Forbush Decrease with GPU parallelization

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DATA AND QUANTUM COMPUTING, SPOKE 3

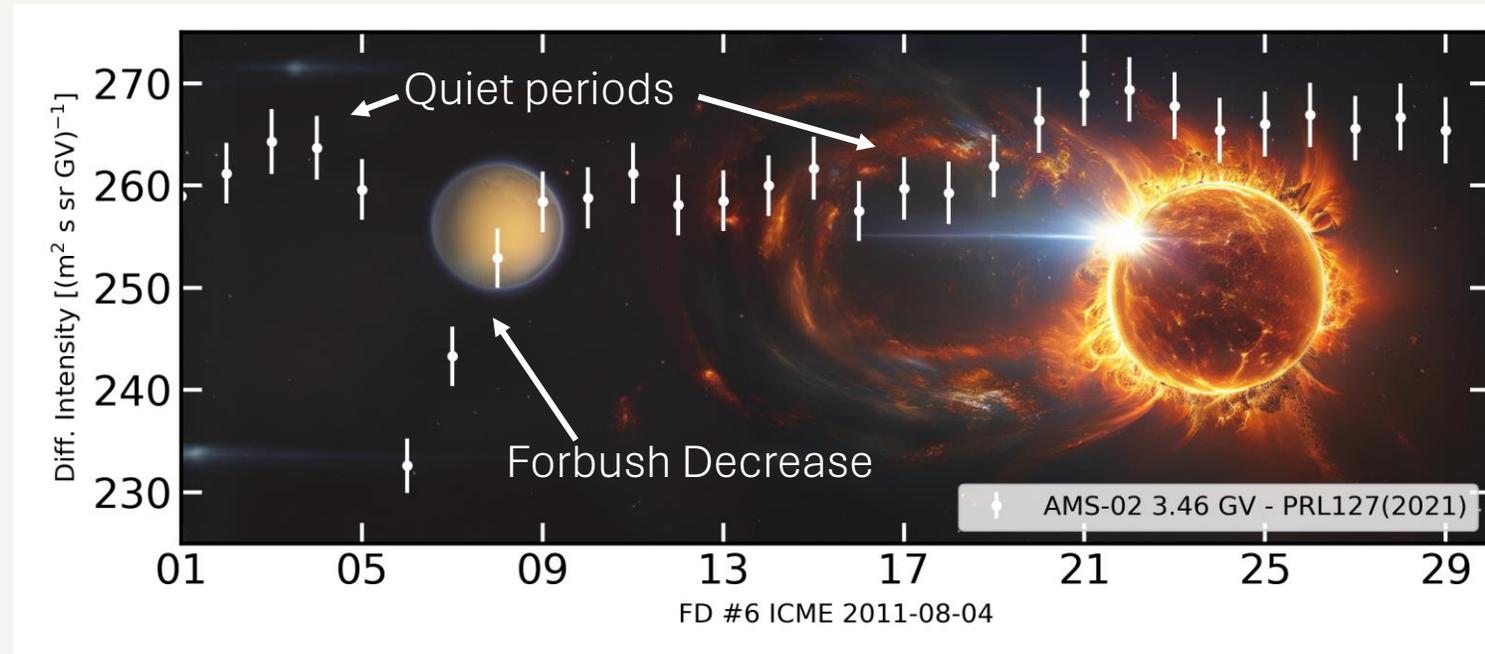
# Scientific Rationale

**Coronal Mass Ejection (CME)** -> expulsion of plasma from the Sun that locally alter the properties of the interplanetary medium.

**Forbush Decrease (FD)** -> a sudden (local) reduction of the Cosmic Rays (CR) intensity due to CME passage that may take several days to be recovered.

AMS-02 measured 142 FD  
(5/2011->10/2019).

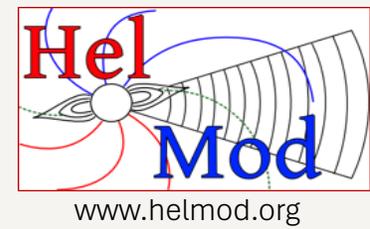
The measured spectra allow for analyzing FD behaviour at different rigidity intervals with unprecedented accuracy.



*Is it possible to infer general properties of particle propagation in the interplanetary medium using a phenomenological approach?*

# The computational model

We use a modified version of



Monte Carlo Code solving a set of Stochastic Differential Equations (SDE) equivalent to Parker Transport Equations.

$$\frac{\partial U}{\partial t} = \underbrace{\frac{\partial}{\partial x_i} \left( K_{ij}^S \frac{\partial U}{\partial x_j} \right)}_{\text{Diffusion}} + \underbrace{\frac{1}{3} \frac{\partial V_{SW,i}}{\partial x_i} \frac{\partial}{\partial T} (\alpha_{rel} T U)}_{\text{Advection}} - \underbrace{\frac{\partial}{\partial x_i} \left[ (V_{SW,i} + v_{d,i}) U \right]}_{\text{Adiabatic loss}} + \underbrace{\left[ (V_{SW,i} + v_{d,i}) U \right]}_{\text{Drift}}$$

Parker Transport Equation  
Fokker-Plank-like equation

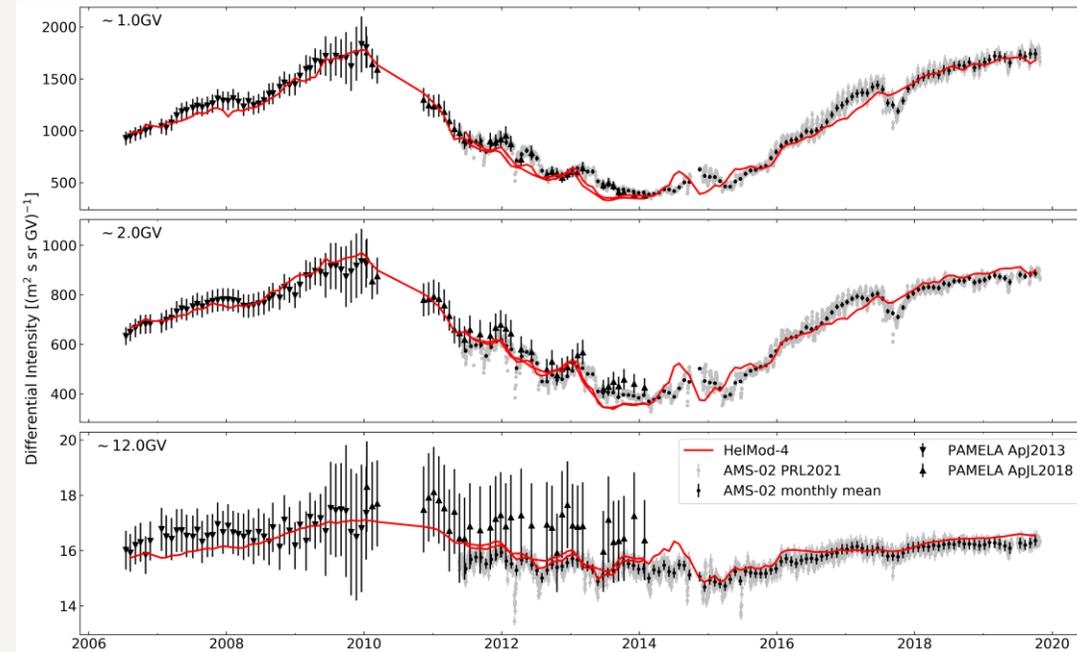
Ito's formula

$$\frac{\partial U}{\partial s} = \sum_i A_{B,i}(s, y) \frac{\partial U}{\partial y_i} + \frac{1}{2} \sum_{i,j} C_{B,ij}(s, y) \frac{\partial^2 U}{\partial y_i \partial y_j} - L_B U + S$$

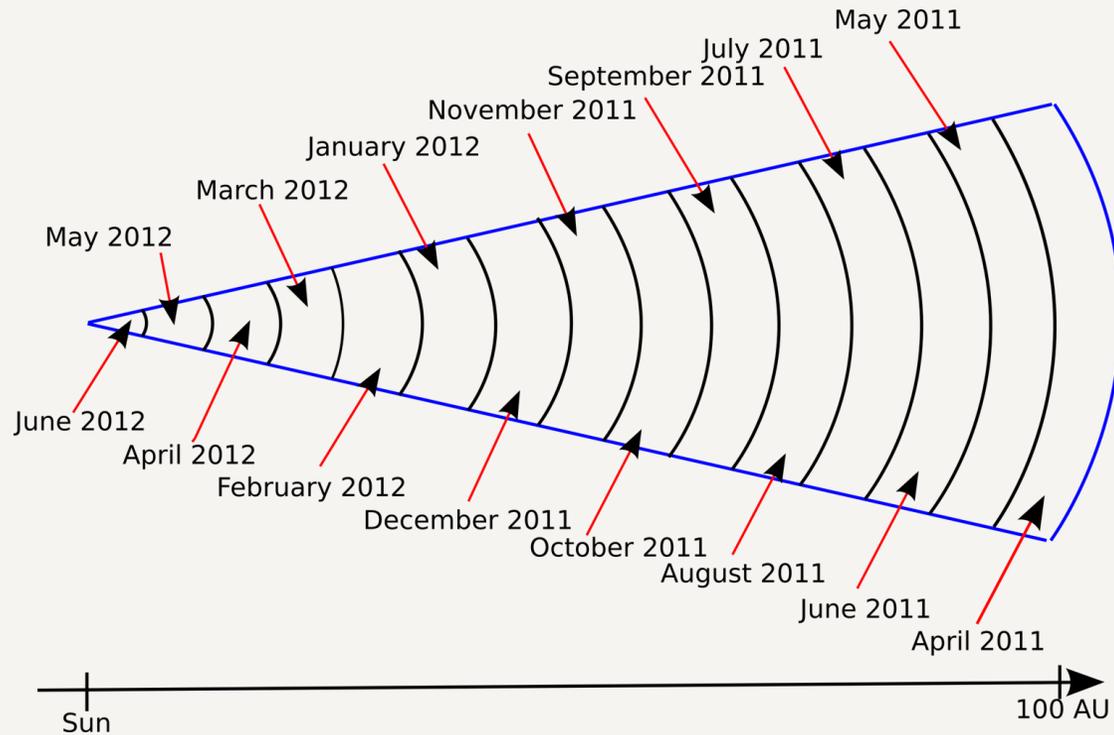
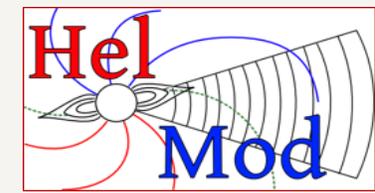
Stochastic Differential Equations

(MC backward in time numerically integrated)

Model parameters are tuned along a complete 22-year solar cycle using CR proton. The same parametrization is then applied to all nuclei.



# The computational model



**We divide the Heliosphere in 15 regions,**  
 each one equivalent to the average of solar activity in the periods before the experiment  
**The Heliosphere radius and shape varies with time,** according with the Sun Activity

Details of the model HelMod-4 (v5.1) can be found in  
*Boschini et al. Adv. Space Res. (2024)*

Parameters in each region are

*Tilt angle of the Neutral Sheet*

*Magnetic Field Magnitude at Earth*

*Solar Wind Speed*

*Diffusion coefficients*

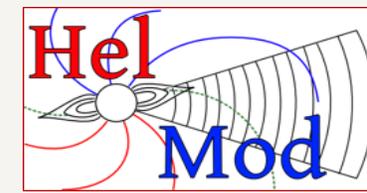
<http://wso.stanford.edu>

<https://omniweb.gsfc.nasa.gov/>

Wilcox Solar Observatory

database

# The computational model

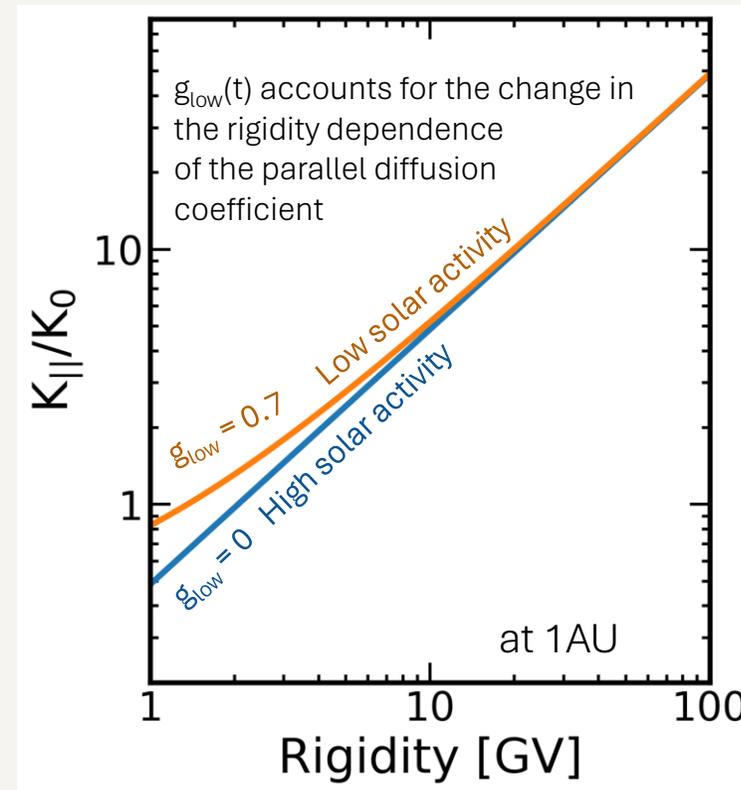
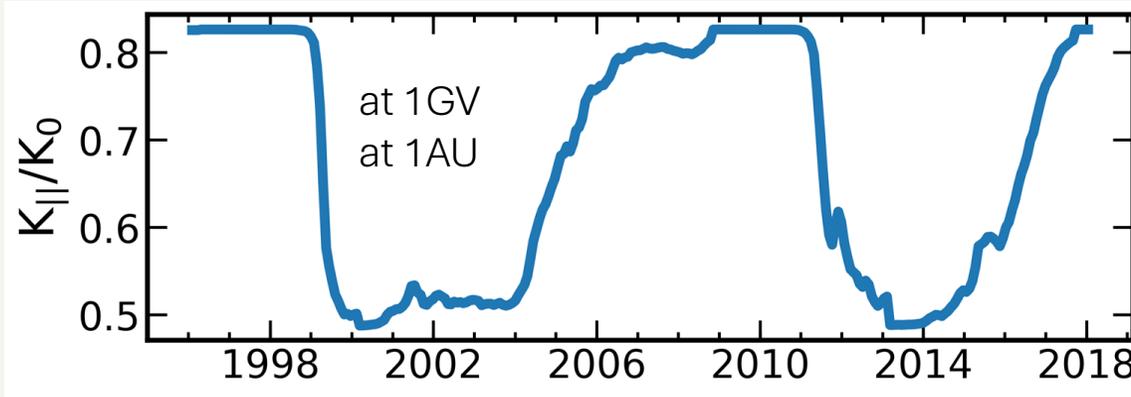


Parametrization of diffusion coefficients:

$$\frac{K_{\parallel}}{K_0} = \frac{\beta}{3} \left[ \frac{P}{1 \text{ GV}} + g_{\text{low}}(t) \right] \left( 1 + \frac{r}{1 \text{ AU}} \right)$$

$$K_{\perp,i} / K_{\parallel} = \rho_i$$

P is rigidity in GV



$K_0(t)$  is the diffusion parameter obtained using cosmic ray fluxes measured with neutron monitor at different latitudes.

see

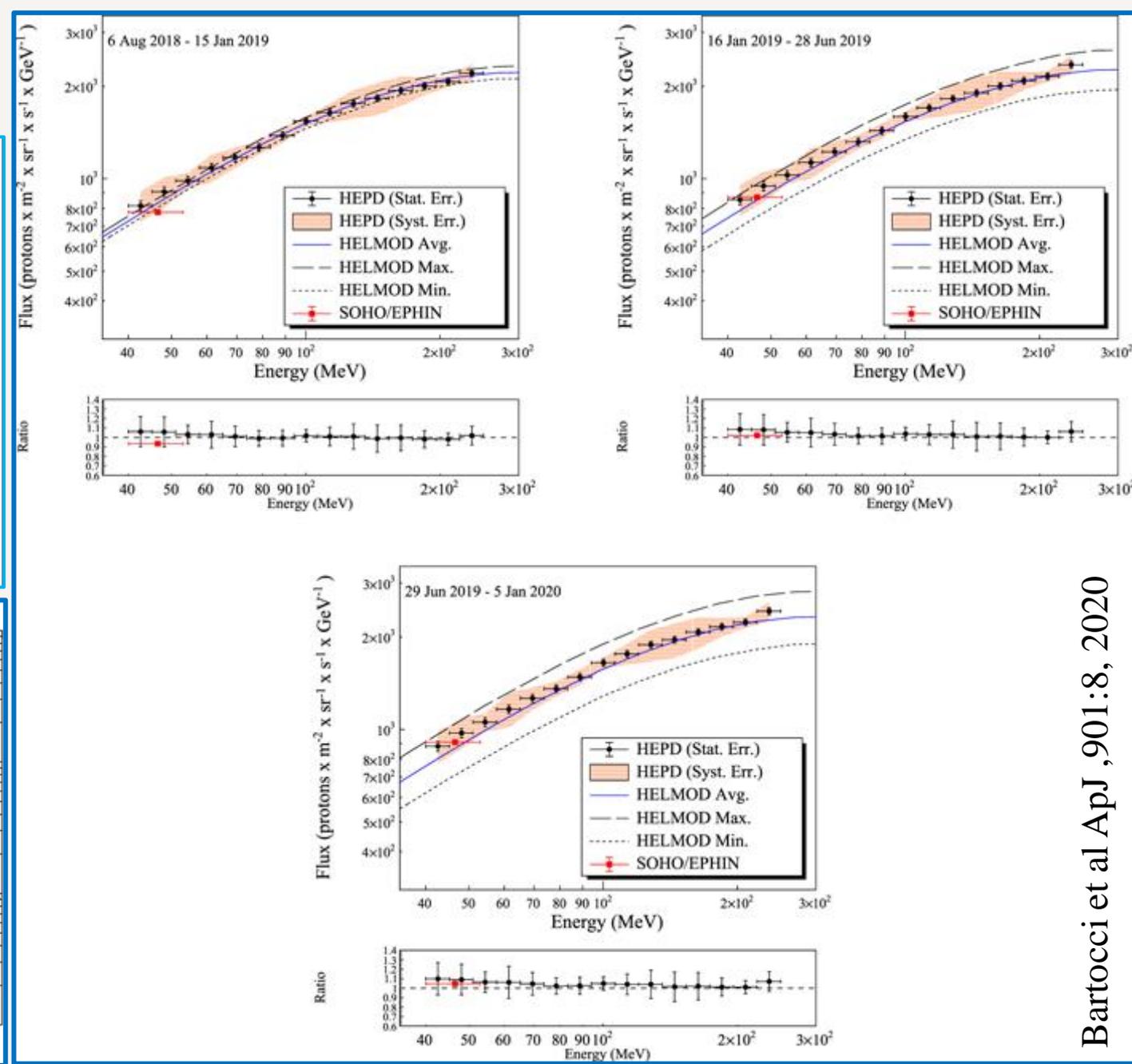
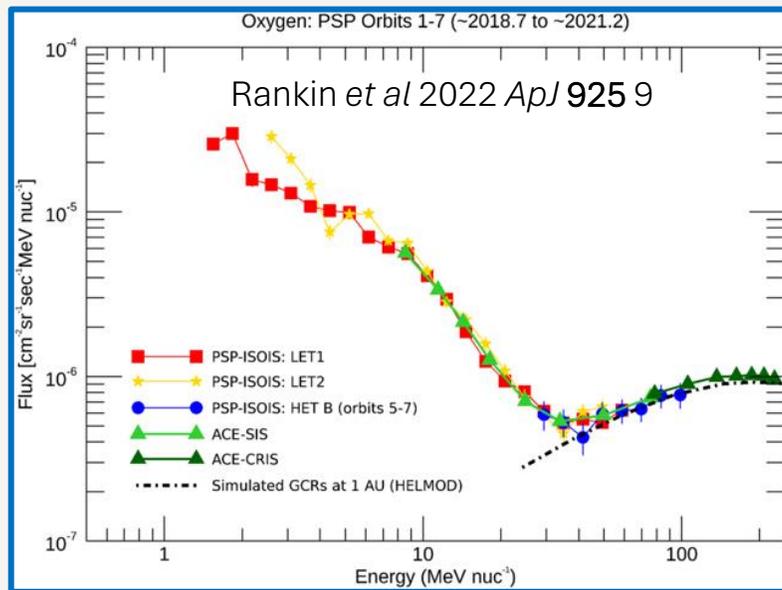
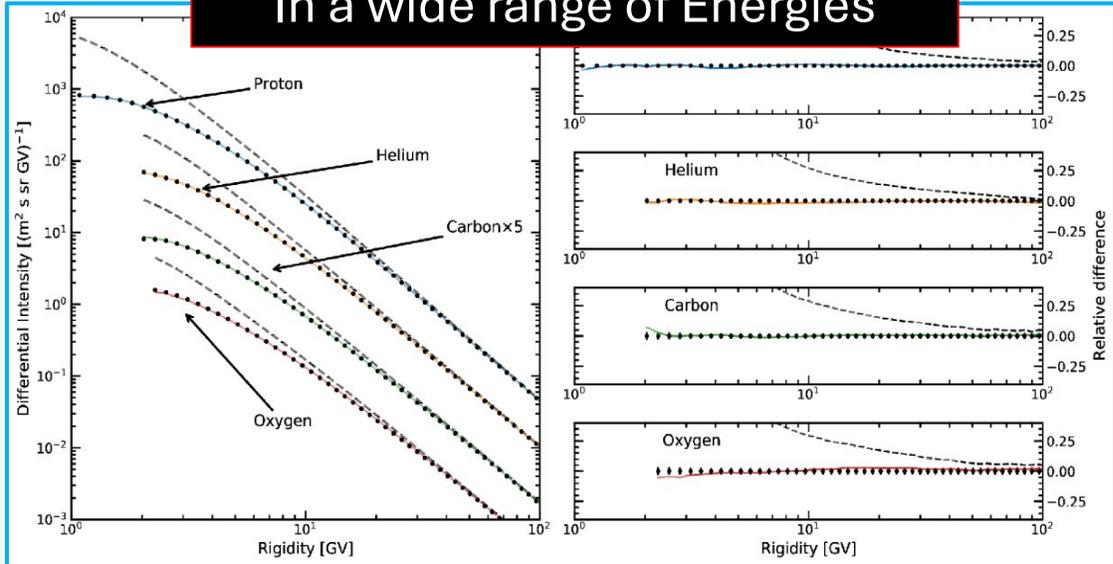
Bobik et al. ApJ 745:132 (2012)

Bobik et al. AdsAst, ID 793072 (2013)

Boschini et al. Adv. S. Res. (2017,2019,2022,2024)

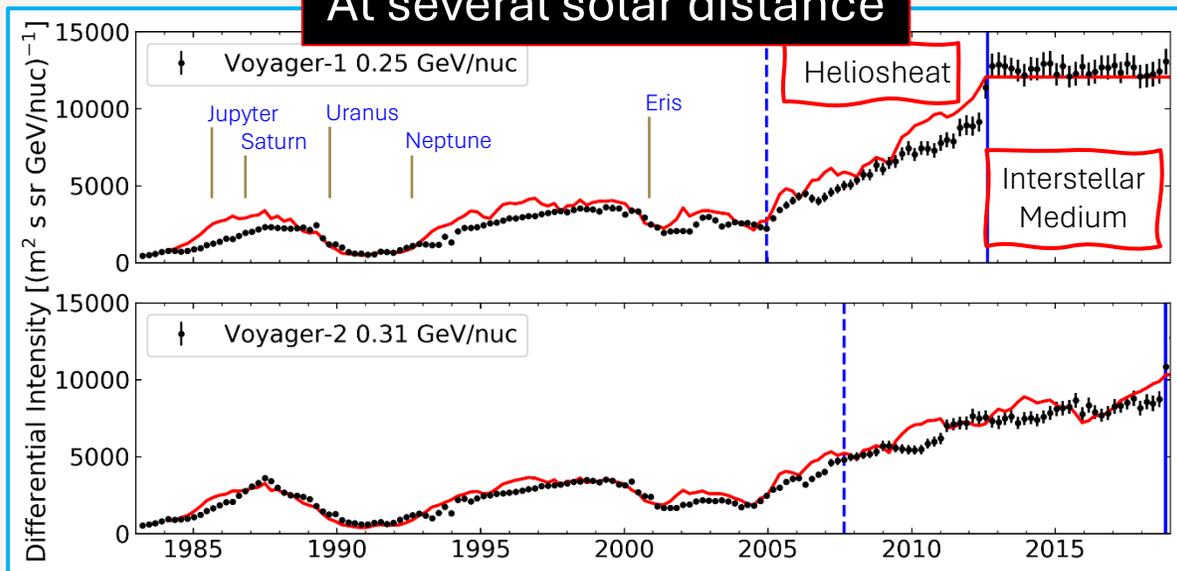
# HelMod reproduces Ions:

In a wide range of Energies

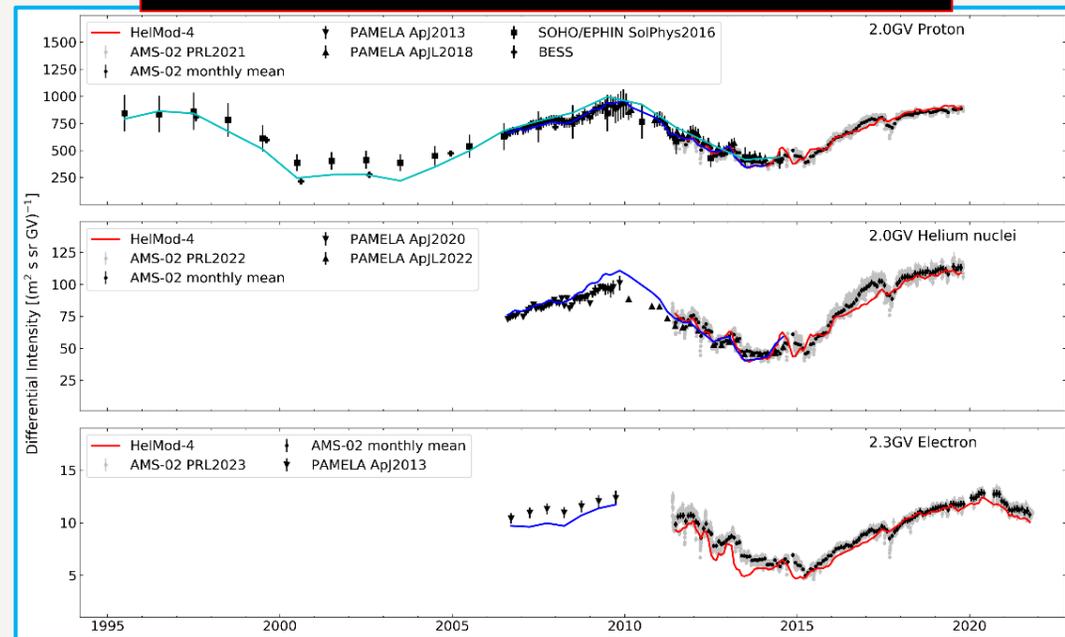


# HelMod reproduces Ions:

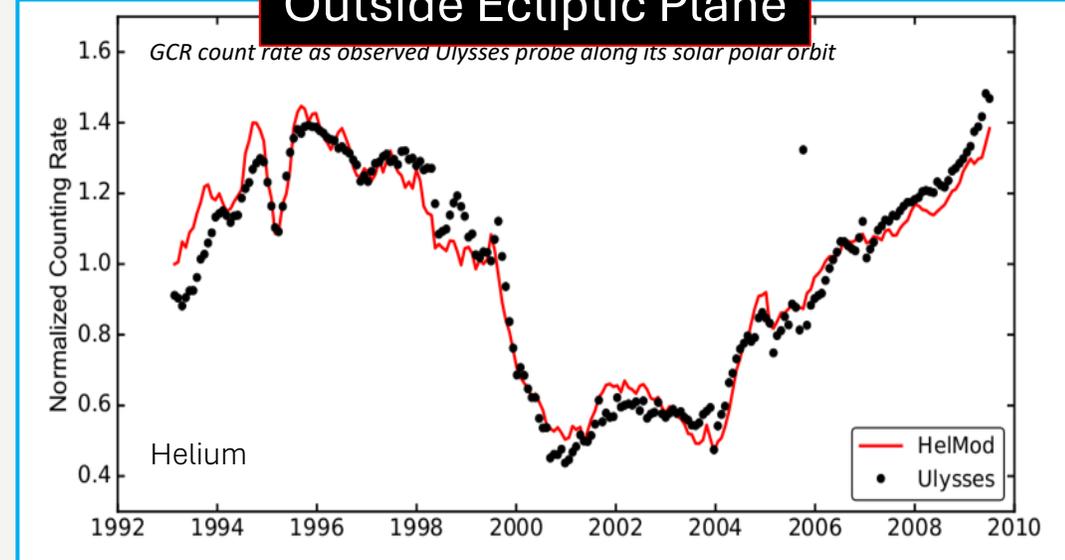
## At several solar distance



## For different solar activities

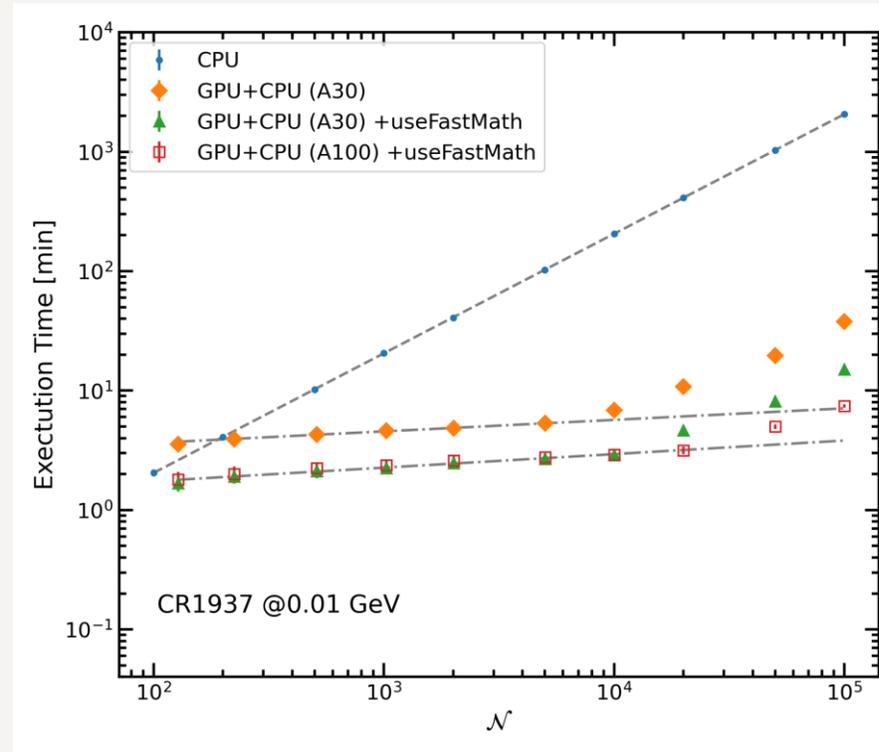
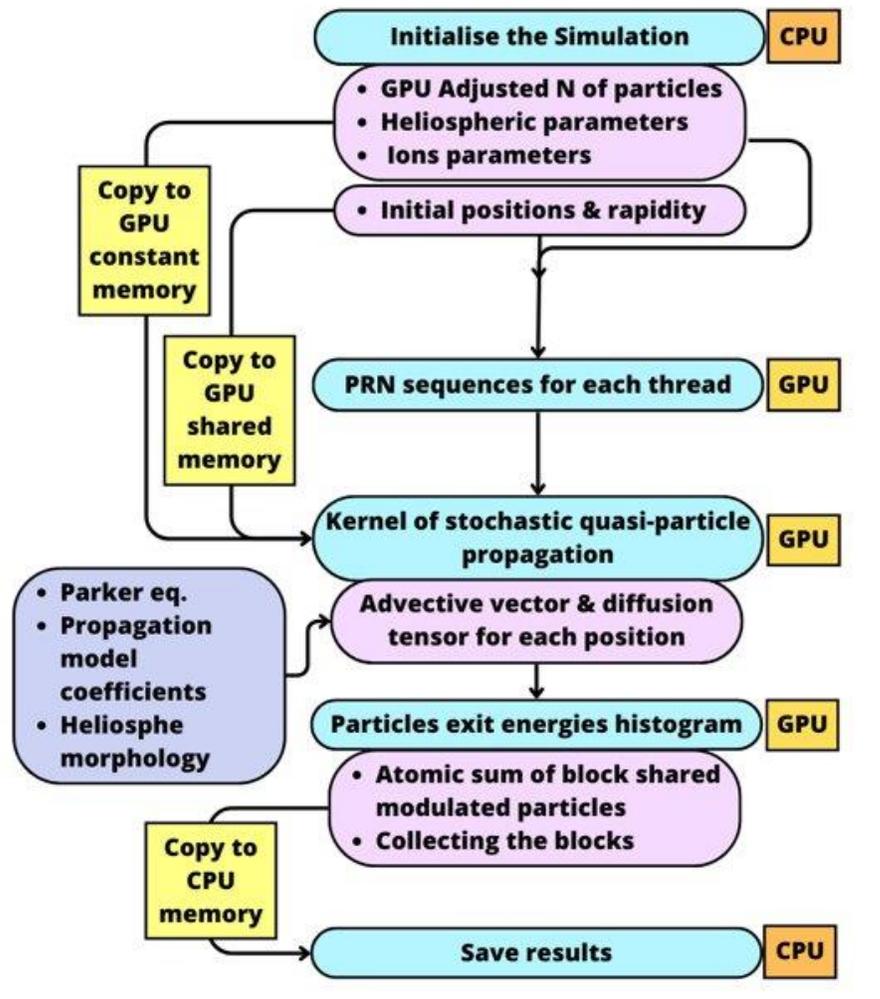


## Outside Ecliptic Plane



# GPU implementation and performances

The SDE integration algorithm is well suited to work with HPC architecture involving GPUs.

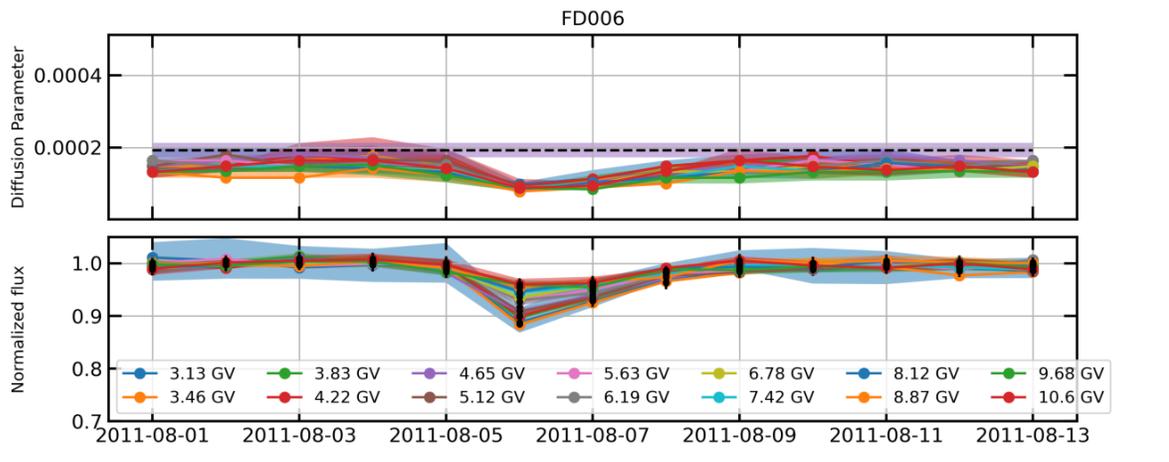


The computational time is dramatically reduced opening to new studies (see Boschini et al 2024). Yet, there is room further to reduce the computational time through code optimization.

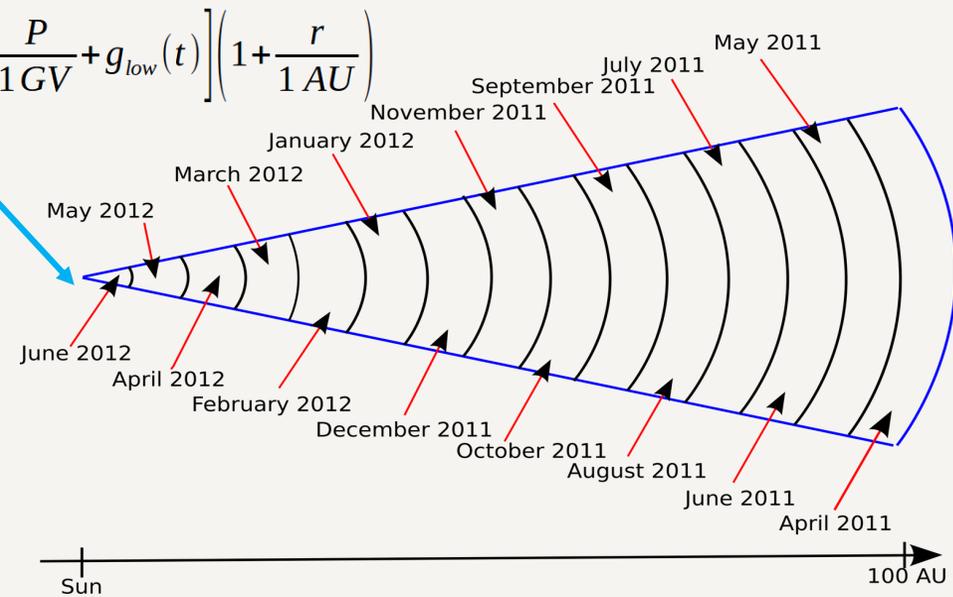
# Methodology

In this work, we modify the value of  $K_0$  parameter in the first shell (i.e.  $\sim 5$  AU) emulating the effect of a local perturbation around Earth and not affecting the rest of the heliosphere

Using a scanning strategy we vary the value of  $K_0$  for each energy and day independently to fit AMS-02 daily spectra from 3 to 10 GV



$$\frac{K_{\parallel}}{K_0} = \frac{\beta}{3} \left[ \frac{P}{1GV} + g_{low}(t) \right] \left( 1 + \frac{r}{1AU} \right)$$



FD	Type	Time	MAR	Ampl
006	ICME	2011/08	16.6	13.6
010	ICME	2011/10	48.5	10.3
017	ICME	2012/03	33.5	35.1
058	ICME	2014/02	33.5	10.0
121	ICME	2017/09	22.8	17.7

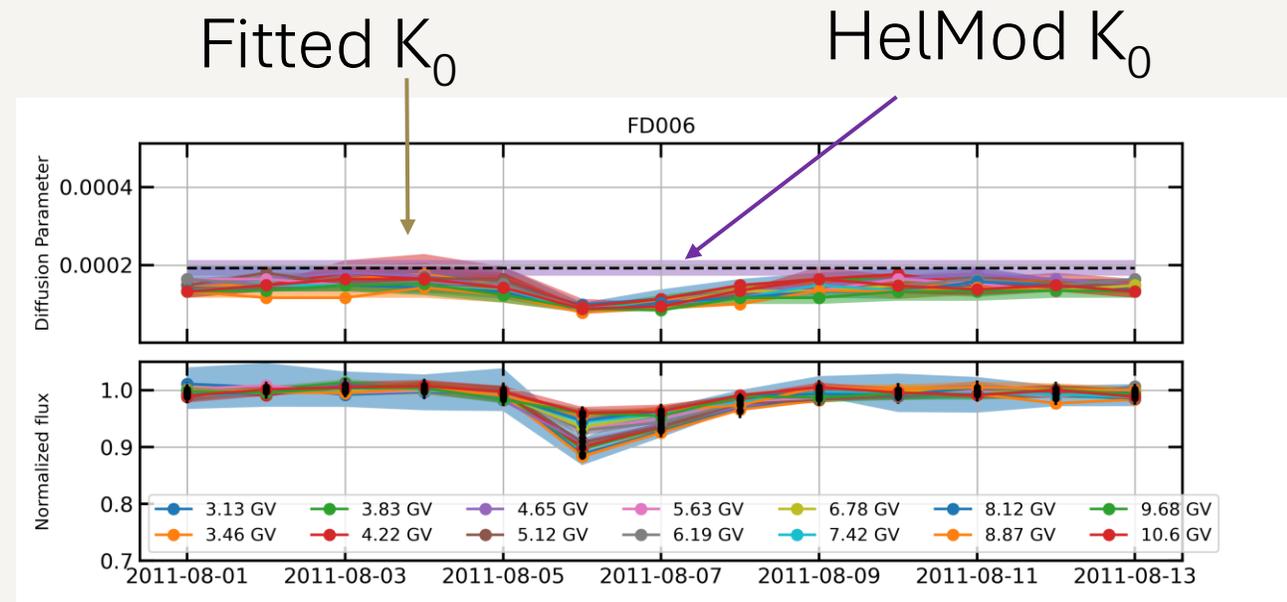
Events from Wang et al ApJ 950:23, 2023.

We apply our study to the five most relevant FD events seen by AMS-02. For each FD we select a time windows that influence up to 4 quiet days before and after the event.

# Preliminary results

We notice that the daily  $K_0$

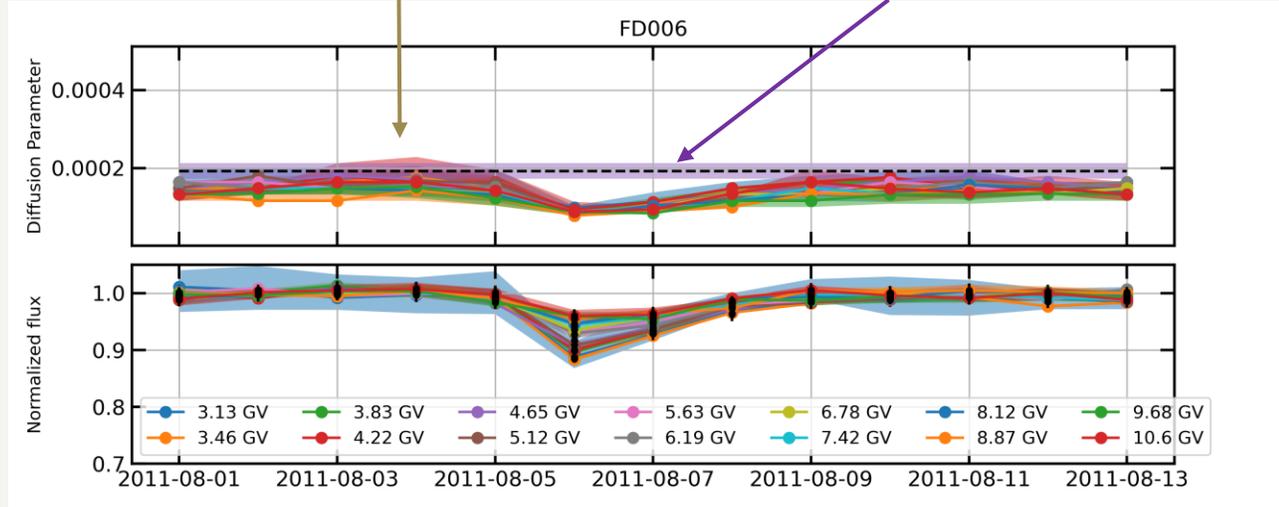
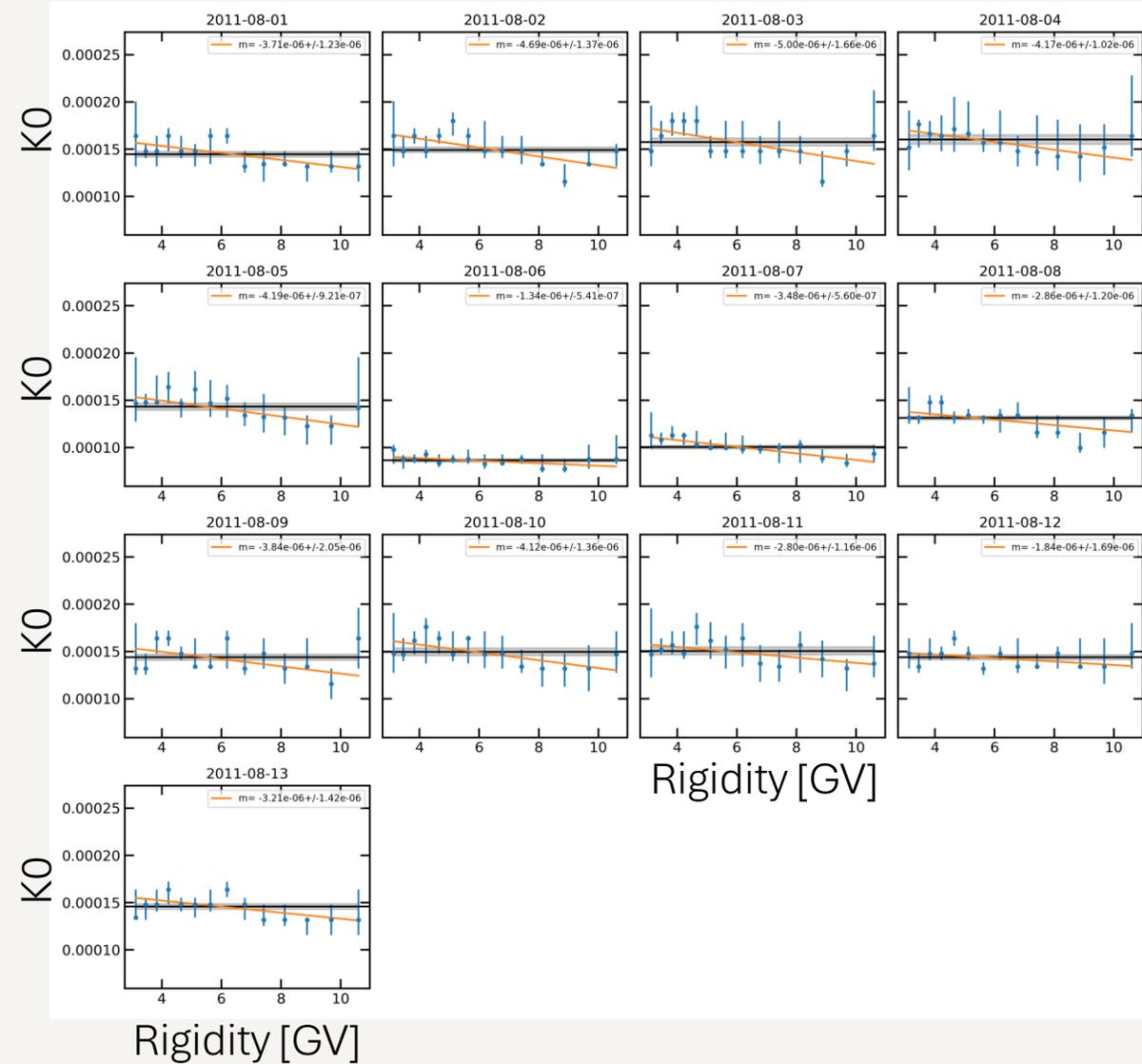
1. decrease following the forrush decrease
2. has similar values for all considered rigidities



Black point = AMS-02 normalized data

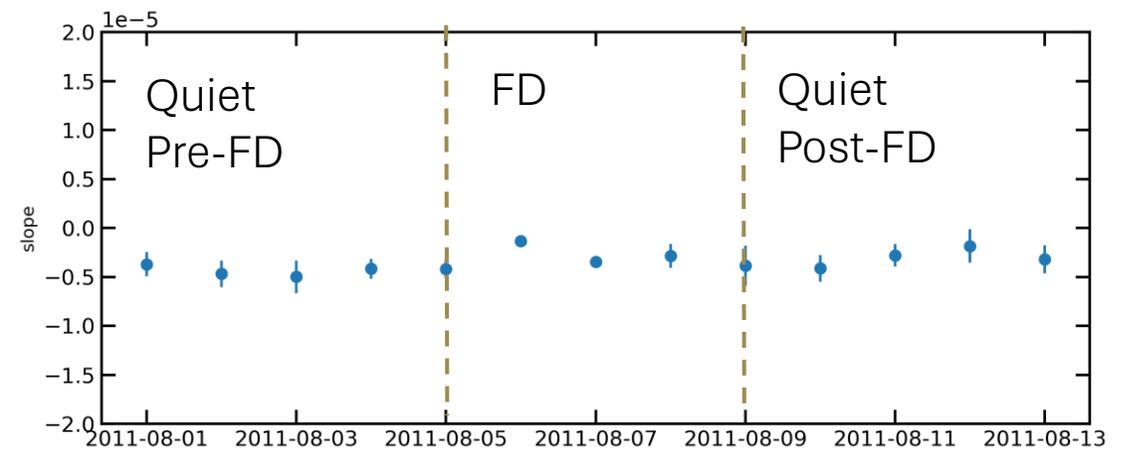
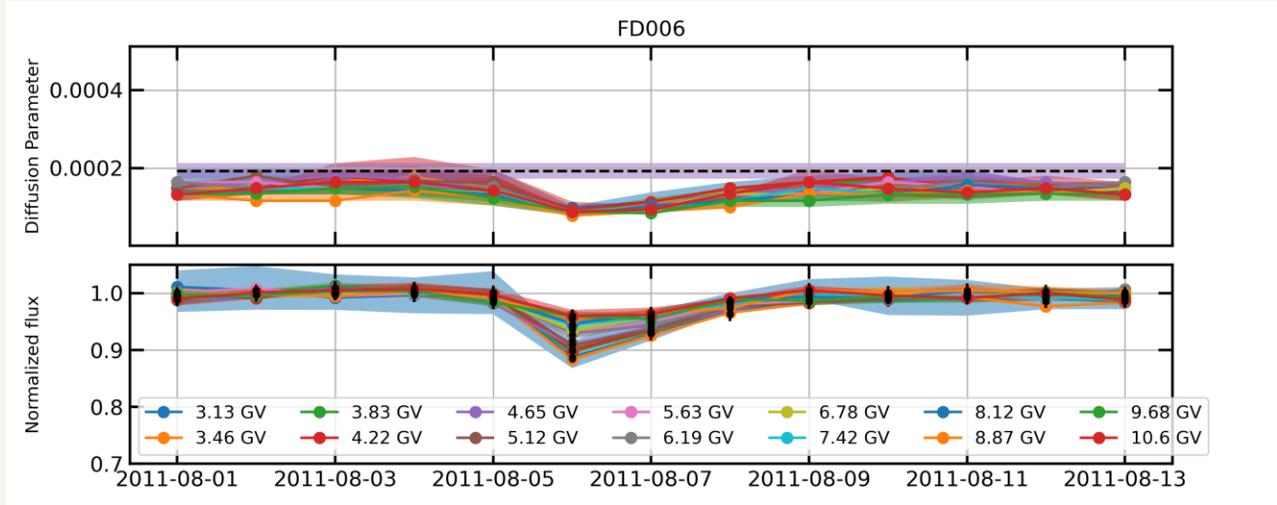
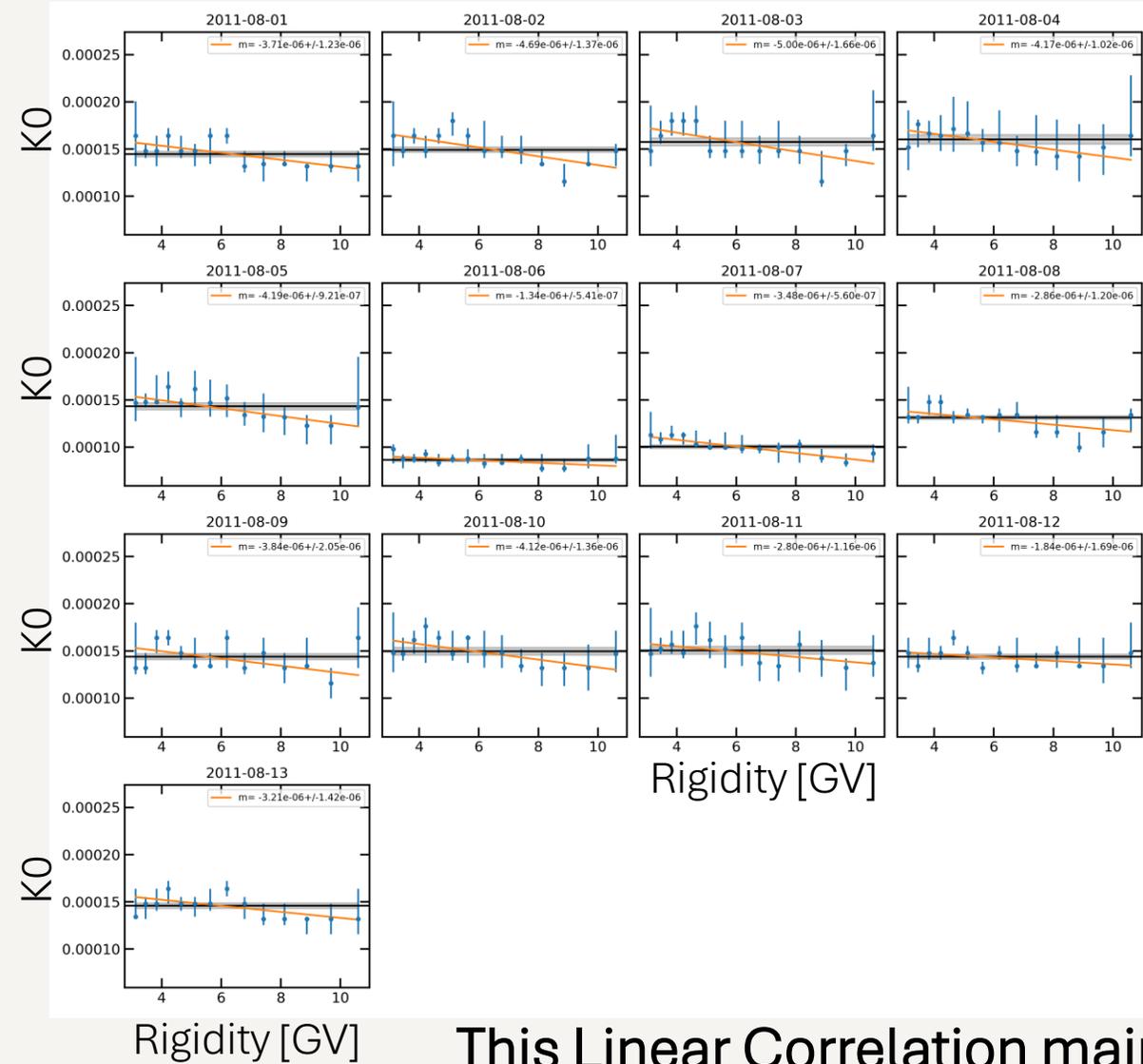
Color band = Simulations best fit

# Preliminary results



We found a linear correlation between  $K_0$  and Rigidity. This may be due to LIS uncertainties or an incorrect rigidity dependence of diffusion tensor.

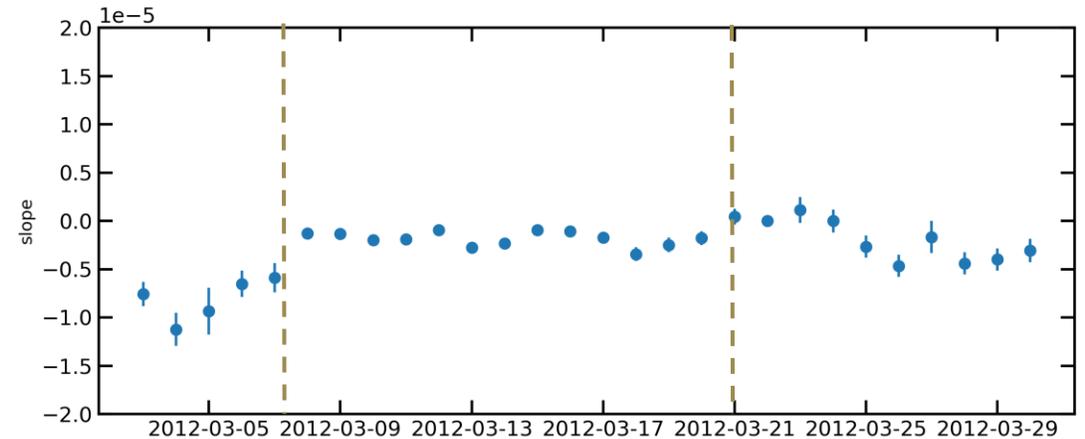
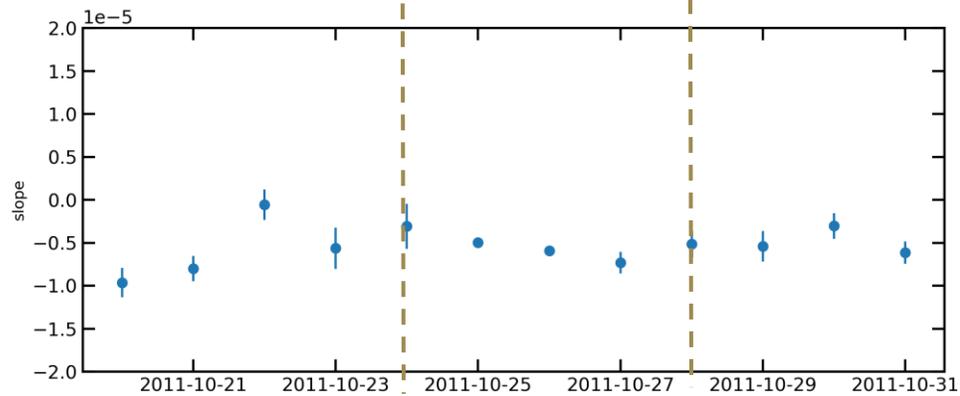
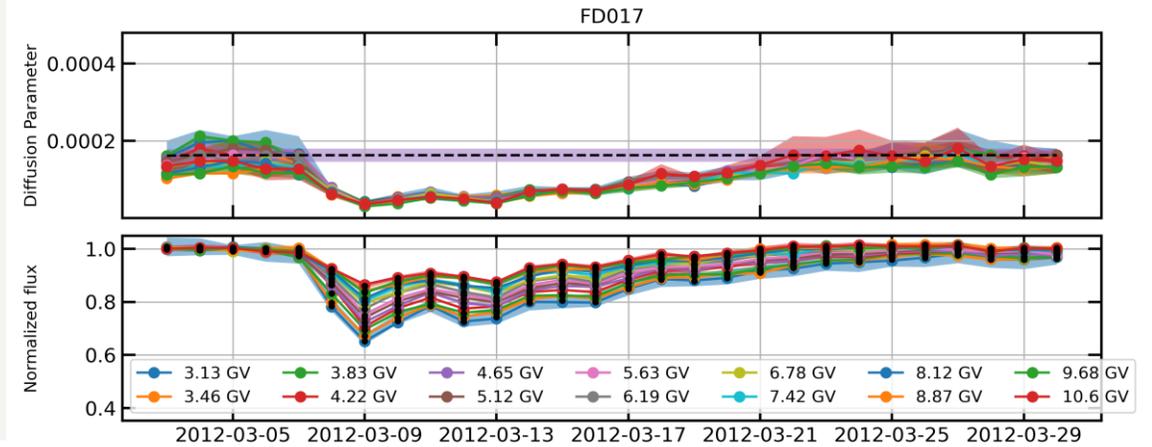
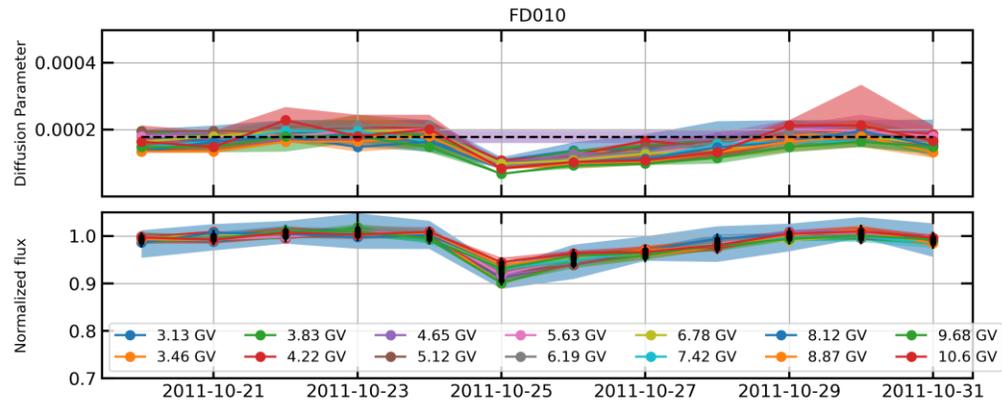
# Preliminary results



This Linear Correlation maintains the same slope both quiet and perturbed days.

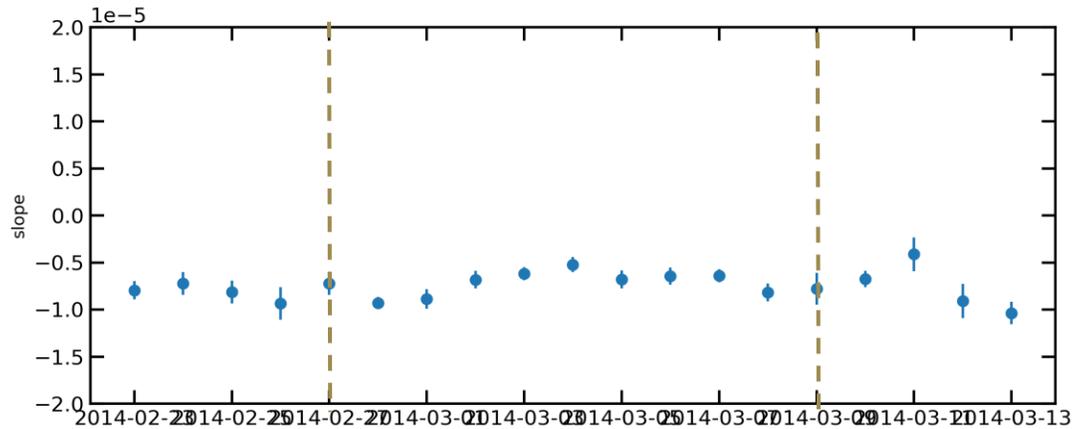
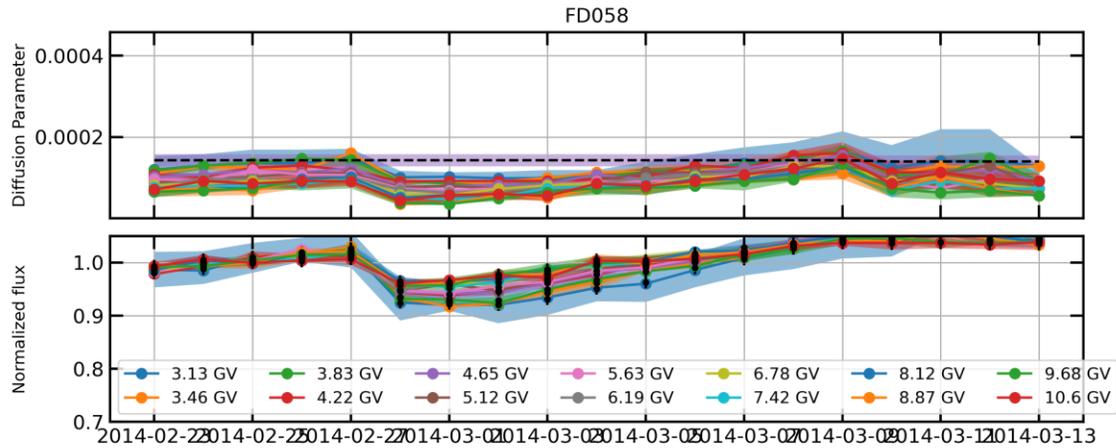
# Preliminary results

Similar results are observed on others FD of the sample

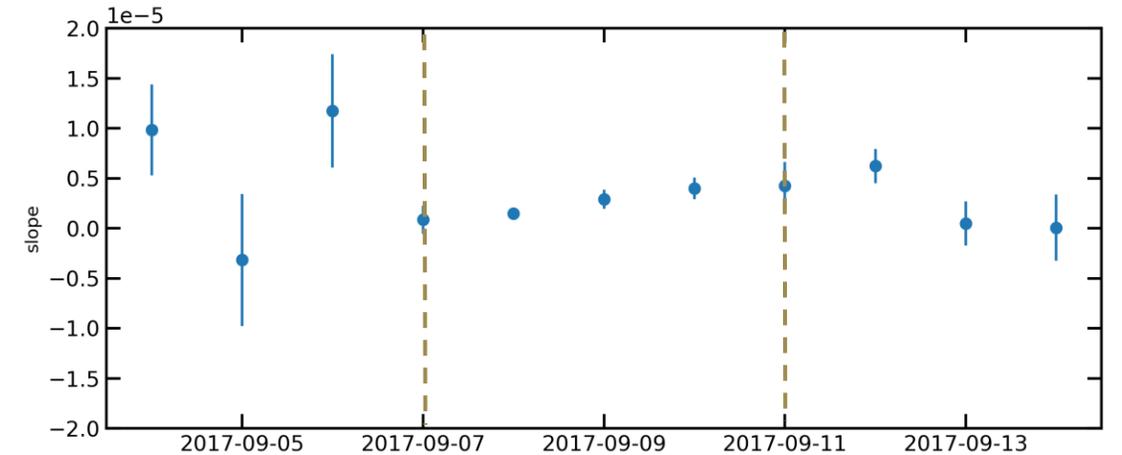
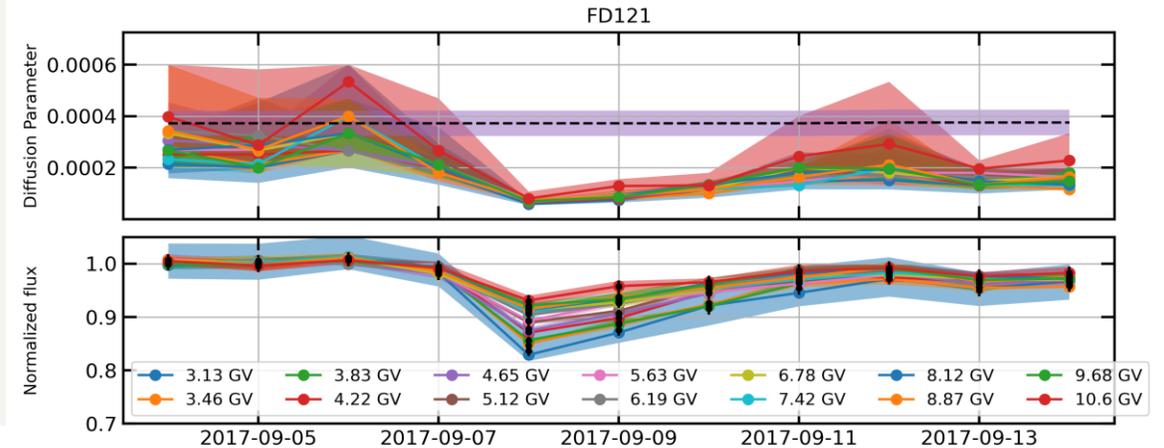


This Linear Correlation maintains the same slope both quiet and perturbed days.

# Preliminary results



Similar results are observed on others FD of the sample



This Linear Correlation maintains the same slope both quiet and perturbed days.

# Comments and Conclusions

- We studied the values change of the diffusion parameter of the HelMod Model during a Forbush Decrease at different rigidities.
- We found similar value of diffusion parameter for different rigidities.
- The relative difference between best  $K_0$  values at different rigidities are not affected by perturbation causing the FD.
- This may be an indication that diffusion tensor description is the same for quiet and perturbed period .
- The study of FD perturbed spectra may allow to inferr general properties of diffusive medium.

Thanks for your attention

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