

**Inferences on mass composition and tests of hadronic interactions
from 0.3 to 100 EeV using the water-Cherenkov detectors
of the Pierre Auger Observatory**

A. Aab,⁷⁸ P. Abreu,⁶⁹ M. Aglietta,^{50,49} I. Al Samarai,³² I. F. M. Albuquerque,¹⁸ I. Allekotte,¹ A. Almela,^{8,11}
J. Alvarez Castillo,⁶⁵ J. Alvarez-Muñiz,⁷⁷ G. A. Anastasi,^{41,43} L. Anchordoqui,⁸⁴ B. Andrada,⁸ S. Andringa,⁶⁹ C. Aramo,⁴⁷
F. Arquerros,⁷⁵ N. Arsene,⁷¹ H. Asorey,^{1,27} P. Assis,⁶⁹ J. Aublin,³² G. Avila,^{9,10} A. M. Badescu,⁷² A. Balaceanu,⁷⁰
F. Barbato,⁵⁷ R. J. Barreira Luz,⁶⁹ J. J. Beatty,⁸⁹ K. H. Becker,³⁴ J. A. Bellido,¹² C. Berat,³³ M. E. Bertaina,^{59,49} X. Bertou,¹
P. L. Biermann,⁹⁴ J. Biteau,³¹ S. G. Blaess,¹² A. Blanco,⁶⁹ J. Blazek,²⁹ C. Bleve,^{53,45} M. Boháčová,²⁹ D. Boncioli,^{43,‡}
C. Bonifazi,²⁴ N. Borodai,⁶⁶ A. M. Botti,^{8,36} J. Brack,⁹⁸ I. Brancus,⁷⁰ T. Bretz,³⁸ A. Bridgeman,³⁶ F. L. Briechele,³⁸
P. Buchholz,⁴⁰ A. Bueno,⁷⁶ S. Buitink,⁷⁸ M. Buscemi,^{55,44} K. S. Caballero-Mora,⁶³ L. Caccianiga,⁵⁶ A. Cancio,^{11,8}
F. Canfora,⁷⁸ L. Caramete,⁷¹ R. Caruso,^{55,44} A. Castellina,^{50,49} F. Catalani,¹⁸ G. Cataldi,⁴⁵ L. Cazon,⁶⁹ A. G. Chavez,⁶⁴
J. A. Chinellato,¹⁹ J. Chudoba,²⁹ R. W. Clay,¹² A. Cobos,⁸ R. Colalillo,^{57,47} A. Coleman,⁹⁰ L. Collica,⁹⁰ M. R. Coluccia,^{53,45}
R. Conceição,⁶⁹ G. Consolati,^{46,51} F. Contreras,^{9,10} M. J. Cooper,¹² S. Coutu,⁹⁰ C. E. Covault,⁸² J. Cronin,⁹¹ S. D'Amico,^{52,45}
B. Daniel,¹⁹ S. Dasso,^{5,3} K. Daumiller,³⁶ B. R. Dawson,¹² R. M. de Almeida,²⁶ S. J. de Jong,^{78,80} G. De Mauro,⁷⁸
J. R. T. de Mello Neto,^{24,25} I. De Mitri,^{53,45} J. de Oliveira,²⁶ V. de Souza,¹⁷ J. Debatin,³⁶ O. Deligny,³¹ M. L. Díaz Castro,¹⁹
F. Diogo,⁶⁹ C. Dobrigkeit,¹⁹ J. C. D'Olivo,⁶⁵ Q. Dorosti,⁴⁰ R. C. dos Anjos,²³ M. T. Dova,⁴ A. Dundovic,³⁹ J. Ebr,²⁹
R. Engel,³⁶ M. Erdmann,³⁸ M. Erfani,⁴⁰ C. O. Escobar,⁹⁶ J. Espadanal,⁶⁹ A. Etchegoyen,^{8,11} H. Falcke,^{78,81,80} J. Farmer,⁹¹
G. Farrar,⁸⁷ A. C. Fauth,¹⁹ N. Fazzini,⁹⁶ F. Fenu,^{59,49} B. Fick,⁸⁶ J. M. Figueira,⁸ A. Filipčič,^{73,74} O. Fratu,⁷² M. M. Freire,⁶
T. Fujii,⁹¹ A. Fuster,^{8,11} R. Gaior,³² B. García,⁷ D. Garcia-Pinto,⁷⁵ F. Gaté,⁹⁵ H. Gemmeke,³⁷ A. Gherghel-Lascu,⁷⁰
P. L. Ghia,³¹ U. Giaccari,²⁴ M. Giammarchi,⁴⁶ M. Giller,⁶⁷ D. Głás,⁶⁸ C. Glaser,³⁸ G. Golup,¹ M. Gómez Berisso,¹
P. F. Gómez Vitale,^{9,10} N. González,^{8,36} A. Gorgi,^{50,49} P. Gorham,⁹⁹ A. F. Grillo,⁴³ T. D. Grubb,¹² F. Guarino,^{57,47}
G. P. Guedes,²⁰ R. Halliday,⁸² M. R. Hampel,⁸ P. Hansen,⁴ D. Harari,¹ T. A. Harrison,¹² J. L. Harton,⁹⁸ A. Haungs,³⁶
T. Hebbeker,³⁸ D. Heck,³⁶ P. Heimann,⁴⁰ A. E. Herve,³⁵ G. C. Hill,¹² C. Hojvat,⁹⁶ E. Holt,^{36,8} P. Homola,⁶⁶
J. R. Hörandel,^{78,80} P. Horvath,³⁰ M. Hrabovský,³⁰ T. Huege,³⁶ J. Hulsman,^{8,36} A. Insolia,^{55,44} P. G. Isar,⁷¹ I. Jandt,³⁴
J. A. Johnsen,⁸³ M. Josebachuili,⁸ J. Juryssek,²⁹ A. Kääpä,³⁴ O. Kambeitz,³⁵ K. H. Kampert,³⁴ B. Keilhauer,³⁶
N. Kemmerich,¹⁸ E. Kemp,¹⁹ J. Kemp,³⁸ R. M. Kieckhafer,⁸⁶ H. O. Klages,³⁶ M. Kleifges,³⁷ J. Kleinfeller,⁹ R. Krause,³⁸
N. Krohm,³⁴ D. Kuempel,³⁸ G. Kukec Mezek,⁷⁴ N. Kunka,³⁷ A. Kuotb Awad,³⁶ B. L. Lago,¹⁵ D. LaHurd,⁸² R. G. Lang,¹⁷
M. Lauscher,³⁸ R. Legumina,⁶⁷ M. A. Leigui de Oliveira,²² A. Letessier-Selvon,³² I. Lhenry-Yvon,³¹ K. Link,³⁵
D. Lo Presti,^{44,55} L. Lopes,⁶⁹ R. López,⁶⁰ A. López Casado,⁷⁷ R. Lorek,⁸² Q. Luce,³¹ A. Lucero,^{8,11} M. Malacari,⁹¹
M. Mallamaci,^{56,46} D. Mandat,²⁹ P. Mantsch,⁹⁶ A. G. Mariazzi,⁴ I. C. Mariş,¹³ G. Marsella,^{53,45} D. Martello,^{53,45}
H. Martinez,⁶¹ O. Martínez Bravo,⁶⁰ J. J. Masías Meza,³ H. J. Mathes,³⁶ S. Mathys,³⁴ J. Matthews,⁸⁵ J. A. J. Matthews,¹⁰⁰
G. Matthiae,³⁴ E. Mayotte,³⁴ P. O. Mazur,⁹⁶ C. Medina,⁸³ G. Medina-Tanco,⁶⁵ D. Melo,⁸ A. Meshnikov,³⁷
K.-D. Merenda,⁸³ S. Michal,³⁰ M. I. Micheletti,⁶ L. Middendorf,³⁸ L. Miramonti,^{56,46} B. Mitrica,⁷⁰ D. Mockler,³⁵
S. Mollerach,¹ F. Montanet,³³ C. Morello,^{50,49} M. Mostafá,⁹⁰ A. L. Müller,^{8,36} G. Müller,³⁸ M. A. Muller,^{19,21} S. Müller,^{36,8}
R. Mussa,⁴⁹ I. Naranjo,¹ L. Nellen,⁶⁵ P. H. Nguyen,¹² M. Niculescu-Oglinzu,⁷⁰ M. Niechciol,⁴⁰ L. Niemiets,³⁴
T. Niggemann,³⁸ D. Nitz,⁸⁶ D. Nosek,²⁸ V. Novotny,²⁸ L. Nožka,³⁰ L. A. Núñez,²⁷ L. Ochilo,⁴⁰ F. Oikonomou,⁹⁰ A. Olinto,⁹¹
M. Palatka,²⁹ J. Pallotta,² P. Papenbreer,³⁴ G. Parente,⁷⁷ A. Parra,⁶⁰ T. Paul,⁸⁴ M. Pech,²⁹ F. Pedreira,⁷⁷ J. Pękala,⁶⁶
R. Pelayo,⁶² J. Peña-Rodríguez,²⁷ L. A. S. Pereira,¹⁹ M. Perlin,⁸ L. Perrone,^{53,45} C. Peters,³⁸ S. Petrera,^{41,43} J. Phuntsok,⁹⁰
R. Piegaia,³ T. Pierog,³⁶ M. Pimenta,⁶⁹ V. Pirronello,^{55,44} M. Platino,⁸ M. Plum,³⁸ C. Porowski,⁶⁶ R. R. Prado,¹⁷
P. Privitera,⁹¹ M. Prouza,²⁹ E. J. Quel,² S. Querchfeld,³⁴ S. Quinn,⁸² R. Ramos-Pollan,²⁷ J. Rautenberg,³⁴ D. Ravnani,⁸
J. Ridky,²⁹ F. Riehn,⁶⁹ M. Risse,⁴⁰ P. Ristori,² V. Rizi,^{54,43} W. Rodrigues de Carvalho,¹⁸ G. Rodriguez Fernandez,^{58,48}
J. Rodriguez Rojo,⁹ D. Rogozin,³⁶ M. J. Roncoroni,⁸ M. Roth,³⁶ E. Roulet,¹ A. C. Rovero,⁵ P. Ruehl,⁴⁰ S. J. Saffi,¹²
A. Saftoiu,⁷⁰ F. Salamida,^{54,43} H. Salazar,⁶⁰ A. Saleh,⁷⁴ F. Salesa Greus,⁹⁰ G. Salina,⁴⁸ F. Sánchez,⁸ P. Sanchez-Lucas,⁷⁶
E. M. Santos,¹⁸ E. Santos,⁸ F. Sarazin,⁸³ R. Sarmiento,⁶⁹ C. Sarmiento-Cano,⁸ R. Sato,⁹ M. Schauer,³⁴ V. Scherini,⁴⁵
H. Schieler,³⁶ M. Schimp,³⁴ D. Schmidt,^{36,8} O. Scholten,^{79,†} P. Schovánek,²⁹ F. G. Schröder,³⁶ S. Schröder,³⁴ A. Schulz,³⁵
J. Schumacher,³⁸ S. J. Sciutto,⁴ A. Segreto,^{42,44} A. Shadkam,⁸⁵ R. C. Shellard,¹⁴ G. Sigl,³⁹ G. Silli,^{8,36} O. Sima,⁹⁷
A. Śmiałkowski,⁶⁷ R. Śmida,³⁶ B. Smith,⁹³ G. R. Snow,⁹² P. Sommers,⁹⁰ S. Sonntag,⁴⁰ R. Squartini,⁹ D. Stanca,⁷⁰
S. Stanič,⁷⁴ J. Stasielak,⁶⁶ P. Stassi,³³ M. Stolpovskiy,³³ F. Strafella,^{53,45} A. Streich,³⁵ F. Suarez,^{8,11} M. Suarez Durán,²⁷
T. Sudholz,¹² T. Suomijärvi,³¹ A. D. Supanitsky,⁵ J. Šupík,³⁰ J. Swain,⁸⁸ Z. Szadkowski,⁶⁸ A. Taboada,³⁵ O. A. Taborda,¹
V. M. Theodoro,¹⁹ C. Timmermans,^{80,78} C. J. Todero Peixoto,¹⁶ L. Tomankova,³⁶ B. Tomé,⁶⁹ G. Torralba Elipse,⁷⁷
P. Travnicek,²⁹ M. Trini,⁷⁴ R. Ulrich,³⁶ M. Unger,³⁶ M. Urban,³⁸ J. F. Valdés Galicia,⁶⁵ I. Valiño,⁷⁷ L. Valore,^{57,47}
G. van Aar,⁷⁸ P. van Bodegom,¹² A. M. van den Berg,⁷⁹ A. van Vliet,⁷⁸ E. Varela,⁶⁰ B. Vargas Cárdenas,⁶⁵ G. Varner,⁹⁹

A. AAB *et al.* R. A. Vázquez,⁷⁷ D. Veberič,³⁶ C. Ventura,²⁵ I. D. Vergara Quispe,⁴ V. Verzi,⁴⁸ J. Vicha,²⁹ L. Villaseñor,⁶⁴ S. Vorobiov,⁷⁴
H. Wahlberg,⁴ O. Wainberg,^{8,11} D. Walz,³⁸ A. A. Watson,⁹³ M. Weber,³⁷ A. Weindl,³⁶ L. Wiencke,⁸³ H. Wilczyński,⁶⁶
C. Wileman,⁹³ M. Wirtz,³⁸ D. Wittkowski,³⁴ B. Wundheiler,⁸ L. Yang,⁷⁴ A. Yushkov,⁸ E. Zas,⁷⁷ D. Zavrtnik,^{74,73}
M. Zavrtnik,^{73,74} A. Zepeda,⁶¹ B. Zimmermann,³⁷ M. Ziolkowski,⁴⁰ Z. Zong,³¹ and F. Zuccarello^{55,44}

(Pierre Auger Collaboration)*

¹*Centro Atómico Bariloche and Instituto Balseiro (CNEA-UNCuyo-CONICET), San Carlos de Bariloche, Argentina*

²*Centro de Investigaciones en Láseres y Aplicaciones, CITEDEF and CONICET, Villa Martelli, Argentina*

³*Departamento de Física and Departamento de Ciencias de la Atmósfera y los Océanos, FCEyN, Universidad de Buenos Aires and CONICET, Buenos Aires, Argentina*

⁴*IFLP, Universidad Nacional de La Plata and CONICET, La Plata, Argentina*

⁵*Instituto de Astronomía y Física del Espacio (IAFE, CONICET-UBA), Buenos Aires, Argentina*

⁶*Instituto de Física de Rosario (IFIR)—CONICET/U.N.R. and Facultad de Ciencias Bioquímicas y Farmacéuticas U.N.R., Rosario, Argentina*

⁷*Instituto de Tecnologías en Detección y Astropartículas (CNEA, CONICET, UNSAM), and Universidad Tecnológica Nacional—Facultad Regional Mendoza (CONICET/CNEA), Mendoza, Argentina*

⁸*Instituto de Tecnologías en Detección y Astropartículas (CNEA, CONICET, UNSAM), Buenos Aires, Argentina*

⁹*Observatorio Pierre Auger, Malargüe, Argentina*

¹⁰*Observatorio Pierre Auger and Comisión Nacional de Energía Atómica, Malargüe, Argentina*

¹¹*Universidad Tecnológica Nacional—Facultad Regional Buenos Aires, Buenos Aires, Argentina*

¹²*University of Adelaide, Adelaide, South Australia, Australia*

¹³*Université Libre de Bruxelles (ULB), Brussels, Belgium*

¹⁴*Centro Brasileiro de Pesquisas Físicas, Rio de Janeiro, RJ, Brazil*

¹⁵*Centro Federal de Educação Tecnológica Celso Suckow da Fonseca, Nova Friburgo, Brazil*

¹⁶*Universidade de São Paulo, Escola de Engenharia de Lorena, Lorena, SP, Brazil*

¹⁷*Universidade de São Paulo, Instituto de Física de São Carlos, São Carlos, SP, Brazil*

¹⁸*Universidade de São Paulo, Instituto de Física, São Paulo, SP, Brazil*

¹⁹*Universidade Estadual de Campinas, IFGW, Campinas, SP, Brazil*

²⁰*Universidade Estadual de Feira de Santana, Feira de Santana, Brazil*

²¹*Universidade Federal de Pelotas, Pelotas, RS, Brazil*

²²*Universidade Federal do ABC, Santo André, SP, Brazil*

²³*Universidade Federal do Paraná, Setor Palotina, Palotina, Brazil*

²⁴*Universidade Federal do Rio de Janeiro, Instituto de Física, Rio de Janeiro, RJ, Brazil*

²⁵*Universidade Federal do Rio de Janeiro (UFRJ), Observatório do Valongo, Rio de Janeiro, RJ, Brazil*

²⁶*Universidade Federal Fluminense, EEIMVR, Volta Redonda, RJ, Brazil*

²⁷*Universidad Industrial de Santander, Bucaramanga, Colombia*

²⁸*Charles University, Faculty of Mathematics and Physics, Institute of Particle and Nuclear Physics, Prague, Czech Republic*

²⁹*Institute of Physics of the Czech Academy of Sciences, Prague, Czech Republic*

³⁰*Palacky University, RCPTM, Olomouc, Czech Republic*

³¹*Institut de Physique Nucléaire d'Orsay (IPNO), Université Paris-Sud, Univ. Paris/Saclay, CNRS-IN2P3, Orsay, France*

³²*Laboratoire de Physique Nucléaire et de Hautes Energies (LPNHE), Universités Paris 6 et Paris 7, CNRS-IN2P3, Paris, France*

³³*Laboratoire de Physique Subatomique et de Cosmologie (LPSC), Université Grenoble-Alpes, CNRS-IN2P3, Grenoble, France*

³⁴*Bergische Universität Wuppertal, Department of Physics, Wuppertal, Germany*

³⁵*Karlsruhe Institute of Technology, Institut für Experimentelle Kernphysik (IEKP), Karlsruhe, Germany*

³⁶*Karlsruhe Institute of Technology, Institut für Kernphysik, Karlsruhe, Germany*

³⁷*Karlsruhe Institute of Technology, Institut für Prozessdatenverarbeitung und Elektronik, Karlsruhe, Germany*

³⁸*RWTH Aachen University, III. Physikalisches Institut A, Aachen, Germany*

³⁹*Universität Hamburg, II. Institut für Theoretische Physik, Hamburg, Germany*

⁴⁰*Universität Siegen, Fachbereich 7 Physik—Experimentelle Teilchenphysik, Siegen, Germany*

⁴¹*Gran Sasso Science Institute (INFN), L'Aquila, Italy*

⁴²*INAF—Istituto di Astrofisica Spaziale e Fisica Cosmica di Palermo, Palermo, Italy*

- ⁴³INFN Laboratori Nazionali del Gran Sasso, Assergi (L'Aquila), Italy
- ⁴⁴INFN, Sezione di Catania, Catania, Italy
- ⁴⁵INFN, Sezione di Lecce, Lecce, Italy
- ⁴⁶INFN, Sezione di Milano, Milano, Italy
- ⁴⁷INFN, Sezione di Napoli, Napoli, Italy
- ⁴⁸INFN, Sezione di Roma "Tor Vergata", Roma, Italy
- ⁴⁹INFN, Sezione di Torino, Torino, Italy
- ⁵⁰Osservatorio Astrofisico di Torino (INAF), Torino, Italy
- ⁵¹Politecnico di Milano, Dipartimento di Scienze e Tecnologie Aerospaziali, Milano, Italy
- ⁵²Università del Salento, Dipartimento di Ingegneria, Lecce, Italy
- ⁵³Università del Salento, Dipartimento di Matematica e Fisica "E. De Giorgi," Lecce, Italy
- ⁵⁴Università dell'Aquila, Dipartimento di Scienze Fisiche e Chimiche, L'Aquila, Italy
- ⁵⁵Università di Catania, Dipartimento di Fisica e Astronomia, Catania, Italy
- ⁵⁶Università di Milano, Dipartimento di Fisica, Milano, Italy
- ⁵⁷Università di Napoli "Federico II", Dipartimento di Fisica "Ettore Pancini," Napoli, Italy
- ⁵⁸Università di Roma "Tor Vergata", Dipartimento di Fisica, Roma, Italy
- ⁵⁹Università Torino, Dipartimento di Fisica, Torino, Italy
- ⁶⁰Benemérita Universidad Autónoma de Puebla, Puebla, México
- ⁶¹Centro de Investigación y de Estudios Avanzados del IPN (CINVESTAV), México, Distrito Federal, México
- ⁶²Unidad Profesional Interdisciplinaria en Ingeniería y Tecnologías Avanzadas del Instituto Politécnico Nacional (UPIITA-IPN), México, Distrito Federal, México
- ⁶³Universidad Autónoma de Chiapas, Tuxtla Gutiérrez, Chiapas, México
- ⁶⁴Universidad Michoacana de San Nicolás de Hidalgo, Morelia, Michoacán, México
- ⁶⁵Universidad Nacional Autónoma de México, México, Distrito Federal, México
- ⁶⁶Institute of Nuclear Physics PAN, Krakow, Poland
- ⁶⁷University of Łódź, Faculty of Astrophysics, Łódź, Poland
- ⁶⁸University of Łódź, Faculty of High-Energy Astrophysics, Łódź, Poland
- ⁶⁹Laboratório de Instrumentação e Física Experimental de Partículas—LIP and Instituto Superior Técnico—IST, Universidade de Lisboa—UL, Lisboa, Portugal
- ⁷⁰"Horia Hulubei" National Institute for Physics and Nuclear Engineering, Bucharest-Magurele, Romania
- ⁷¹Institute of Space Science, Bucharest-Magurele, Romania
- ⁷²University Politehnica of Bucharest, Bucharest, Romania
- ⁷³Experimental Particle Physics Department, J. Stefan Institute, Ljubljana, Slovenia
- ⁷⁴Center for Astrophysics and Cosmology (CAC), University of Nova Gorica, Nova Gorica, Slovenia
- ⁷⁵Universidad Complutense de Madrid, Madrid, Spain
- ⁷⁶Universidad de Granada and C.A.F.P.E., Granada, Spain
- ⁷⁷Universidad de Santiago de Compostela, Santiago de Compostela, Spain
- ⁷⁸IMAPP, Radboud University Nijmegen, Nijmegen, Netherlands
- ⁷⁹KVI—Center for Advanced Radiation Technology, University of Groningen, Groningen, Netherlands
- ⁸⁰Nationaal Instituut voor Kernfysica en Hoge Energie Fysica (NIKHEF), Science Park, Amsterdam, Netherlands
- ⁸¹Stichting Astronomisch Onderzoek in Nederland (ASTRON), Dwingeloo, Netherlands
- ⁸²Case Western Reserve University, Cleveland, Ohio, USA
- ⁸³Colorado School of Mines, Golden, Colorado, USA
- ⁸⁴Department of Physics and Astronomy, Lehman College, City University of New York, Bronx, New York, USA
- ⁸⁵Louisiana State University, Baton Rouge, Louisiana, USA
- ⁸⁶Michigan Technological University, Houghton, Michigan, USA
- ⁸⁷New York University, New York, New York, USA
- ⁸⁸Northeastern University, Boston, Massachusetts, USA
- ⁸⁹Ohio State University, Columbus, Ohio, USA
- ⁹⁰Pennsylvania State University, University Park, Pennsylvania, USA
- ⁹¹University of Chicago, Enrico Fermi Institute, Chicago, Illinois, USA
- ⁹²University of Nebraska, Lincoln, Nebraska, USA
- ⁹³School of Physics and Astronomy, University of Leeds, Leeds, United Kingdom
- ⁹⁴Max-Planck-Institut für Radioastronomie, Bonn, Germany
- ⁹⁵SUBATECH, École des Mines de Nantes, CNRS-IN2P3, Université de Nantes, France
- ⁹⁶Fermi National Accelerator Laboratory, Batavia, Illinois, USA
- ⁹⁷University of Bucharest, Physics Department, Bucharest, Romania
- ⁹⁸Colorado State University, Fort Collins, Colorado, USA

We present a new method for probing the hadronic interaction models at ultrahigh energy and extracting details about mass composition. This is done using the time profiles of the signals recorded with the water-Cherenkov detectors of the Pierre Auger Observatory. The profiles arise from a mix of the muon and electromagnetic components of air showers. Using the risetimes of the recorded signals, we define a new parameter, which we use to compare our observations with predictions from simulations. We find, first, inconsistencies between our data and predictions over a greater energy range and with substantially more events than in previous studies. Second, by calibrating the new parameter with fluorescence measurements from observations made at the Auger Observatory, we can infer the depth of shower maximum X_{\max} for a sample of over 81,000 events extending from 0.3 to over 100 EeV. Above 30 EeV, the sample is nearly 14 times larger than what is currently available from fluorescence measurements and extending the covered energy range by half a decade. The energy dependence of $\langle X_{\max} \rangle$ is compared to simulations and interpreted in terms of the mean of the logarithmic mass. We find good agreement with previous work and extend the measurement of the mean depth of shower maximum to greater energies than before, reducing significantly the statistical uncertainty associated with the inferences about mass composition.

I. INTRODUCTION

Our understanding of the properties of the highest-energy cosmic rays has grown enormously over the last 12 years with the advent of data from the Pierre Auger Observatory and the Telescope Array. These devices have been used to study the energy spectrum, the mass composition, and the distribution of arrival directions of cosmic rays from 0.3 to energies beyond 10 EeV. While the features of the energy spectrum and of the arrival directions have been well characterized up to ~ 100 EeV, the situation with regard to the mass spectrum is less satisfactory because of the reliance on models of the hadronic physics. This state of affairs has arisen for two reasons. First, the method that provides the best resolution, and therefore is the most potent for measuring a mass-sensitive feature of extensive air showers, is the fluorescence technique. It has been exploited on an event-by-event basis to determine the depth of shower maximum, i.e., the depth in the atmosphere at which the energy deposition in the shower is greatest, but as observations are restricted to clear moonless nights, the number of events is limited. For example, in the Auger data so far reported (up to December 31, 2012), there are 227 events above 16 EeV [1]. For the same energy range, the event number from the Telescope Array is smaller, 25 [2]. Second, to interpret the data sets from the water-Cherenkov detectors and the fluorescence telescopes, one must use the predictions of features of hadronic interactions, such as the cross sections for proton and pion interactions, the multiplicity and the inelasticity, at center-of-mass energies up to ~ 300 TeV, well beyond what is accessible at the LHC [3].

To overcome the limitations imposed by the relatively small number of events accumulated with the fluorescence technique at the highest energies, use can be made of data recorded with the water-Cherenkov detectors of the Observatory that are operational nearly 100% of the time and thus yield substantially more events at a given energy. In this paper, we describe a new method for extracting information about the development of air showers from the time profiles of the signals from the water-Cherenkov detectors.

Our method allows a comparison of the data with predictions from models of parameters inferred directly from these detectors in which a signal from a mix of the muon and electromagnetic components of air showers is available. This approach follows the line opened in four recent studies. From comparisons of Auger observations with hadronic models, it is argued that the latter are inadequate to describe the various measurements [4–7]. As in the earlier work, we find that there are inconsistencies between the models and the data; this is established over a greater energy range and with more events than before.

The method also enables us to infer the depth of shower maximum (a dominantly electromagnetic measurement) by calibrating the new parameter with measurements from the fluorescence telescopes. We have determined X_{\max} for about three times more events than what is available from these telescopes alone over the range from ~ 0.3 to beyond 70 EeV; specifically for the two surface-detector configurations, the 750 and 1500 m arrays [8], there are 27553 and 54022 events recorded, respectively, for which estimates of X_{\max} have been possible. Of those, 49 events are in the range beyond 70 EeV, and 1586 events are in the range above 20 EeV.

The structure of the paper is as follows. In Sec. II, features of the Pierre Auger Observatory are briefly outlined. The measurement of the risetime of signals from the

* auger_spokespersons@fnal.gov; <http://www.auger.org>.

† Also at Vrije Universiteit Brussels, Brussels, Belgium.

‡ Now at Deutsches Elektronen-Synchrotron (DESY), Zeuthen, Germany.

water-Cherenkov detectors is described in Sec. III, and the new parameter for studying the depth of shower maximum is introduced in Sec. IV. A comparison of the new parameter with predictions from hadronic models is discussed in Sec. V. Section VI presents the results on the measurement of average X_{\max} from 0.3 to beyond 70 EeV. A summary of the conclusions is given in Sec. VII.

II. PIERRE AUGER OBSERVATORY

The Pierre Auger Observatory is located near the city of Malargüe in the province of Mendoza, Argentina. It is a hybrid system, being a combination of a large array of surface detectors and a set of fluorescence detectors, used to study cosmic rays with energies above 0.1 EeV. Full details of the instrumentation and the methods used for event reconstruction are given in Ref. [8].

The work presented here is based on data gathered from January 1, 2004, to December 31, 2014, from the surface-detector array (SD), which covers an area of over 3000 km². The array contains 1660 water-Cherenkov detectors, 1600 of which are deployed on a hexagonal grid with 1500 m spacing with the remainder on a lattice of 750 m covering 23.5 km². We refer to these configurations as the 1500 m and 750 m arrays. The water-Cherenkov detectors are used to sample the electromagnetic and muonic components of extensive air showers. Each detector contains 12 metric tons of ultrapure water in a cylindrical container, lined with Tyvec, 1.2 m deep and of 10 m² area. The water is viewed by three 9 in. photomultiplier tubes (PMTs). Signals from the anode and an amplified signal from the last dynode of each PMT are digitized using 40 MHz 10 bit flash analog to digital converters (FADCs); these are called the “high-gain” and “low-gain” channels in what follows. The responses of the detectors are calibrated in units of the signal produced by a muon traversing the water vertically at the center of the station; this unit is termed the “vertical equivalent muon” (VEM) [9]. Air showers are identified using a threefold coincidence, satisfied when a triangle of neighboring stations is triggered [10]. Using the six FADCs, 768 samples (over 19.2 μ s) are recorded at each triggered station. For the present analysis, events that are confined within the array so that an accurate reconstruction is ensured are used. This requires that all six stations of the hexagon surrounding the detector with the highest signal are operational and is known as the 6T5 condition. The arrival directions are found from the relative arrival times of the shower front at the triggered stations. The angular resolution is 0.8° for energies above 3 EeV for the 1500 m array and 1° for the 750 m configuration [8].

The estimator of the primary energy is the signal reconstructed at 1000 m (1500 m array) or 450 m (750 m array) from the shower core, denoted by $S(1000)$ and $S(450)$, respectively. These estimators are determined, together with the core position, through a fit of the recorded signals (converted to units of VEM after integration of the FADC traces) to a lateral distribution function that describes the

average rate of fall-off of the signals as a function of the distance from the shower core. For $S(1000) > 20$ VEM (corresponding to an energy of ~ 3 EeV), showers are recorded with full efficiency over the whole area of the array. For the 750 m array, the corresponding value of $S(450)$ for full efficiency is ~ 60 VEM (~ 0.5 EeV). The accuracy of the core location in lateral distance is ~ 50 m (35 m) for the two configurations. The uncertainty of $S(1000)$, which is insensitive to the lateral distribution function [11], is 12% (3%) at 3 EeV (10 EeV), and for $S(450)$, the corresponding figure is 30% at 0.5 EeV.

The conversions from $S(450)$ and $S(1000)$ to energy are derived using subsets of showers that trigger the fluorescence detector and the surface array independently (“hybrid events”) using well-established methods [12]. The statistical uncertainty in the energy determination is about 16% (12%) for the two reference energies of the 1500 m array and 15% at 0.5 EeV for the 750 m array. The absolute energy scale, determined using the fluorescence detector, has a systematic uncertainty of 14% [13].

Twenty-four telescopes (each with a field of view of $30^\circ \times 30^\circ$) form the fluorescence detector (FD). They are distributed in sets of six at four observation sites. The FD overlooks the SD array and collects the fluorescence light produced as the shower develops in the atmosphere. Its duty cycle amounts to $\sim 15\%$ since it operates exclusively on clear moonless nights. The 750 m array is overlooked from one observation site by three high-elevation telescopes (HEAT) with a field of view covering elevations from 30° to 60° , thus allowing the study of lower-energy showers. Those low-energy showers are detected closer to the detector; therefore, we need a higher elevation field of view to contain also this kind of events.

III. RISETIME AND ITS MEASUREMENT

A. Overview of the risetime concept

In the study described below, we use the risetime of the signals from the water-Cherenkov detectors to extract information about the development of showers. A single parameter, namely, the time for the signal to increase from 10% to 50% of the final magnitude of the integrated signal, $t_{1/2}$, is used to characterize the signal at each station. This parameter was used for the first demonstration of the existence of “between-shower” fluctuations in an early attempt to get information about the mass of the cosmic rays at ~ 1 EeV [14]. That work was carried out using data from the Haverah Park array in England, where the water-Cherenkov detectors were of 1.2 m deep (identical to those of the Auger Observatory) and of area 34 m².

The choice of this parameter is based on the experimental work by Linsley and Scarsi [15]. They showed that at distances of more than about 100 m from the shower core the early part of the shower signal is dominated by muons. Direct measurements of muons using magnetic spectrographs established that the mean momentum of muons

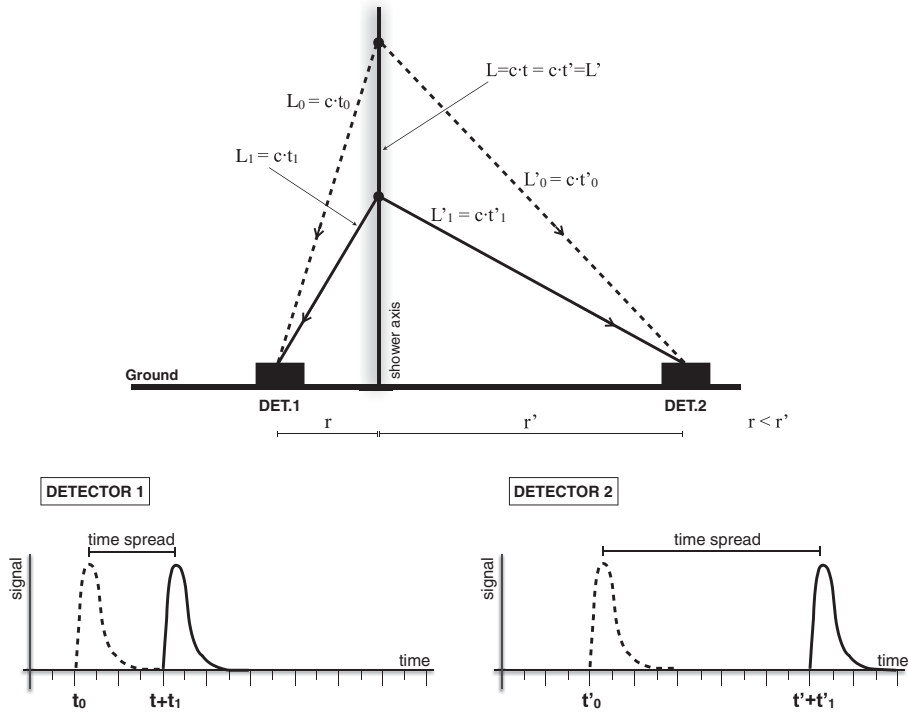


FIG. 1. Qualitative sketch of how geometrical effects affect the temporal spread of the muons at a detector.

beyond 100 m was more than 1 GeV; this leads to the conclusion that the geometrical effects dominate the temporal spread of the muons at a detector. This is illustrated in Fig. 1 for a shower arriving in the vertical direction where it can be seen that the muons arriving from lower down in the shower arrive later at a detector than those that arise from higher up. Furthermore, it is evident that at larger distances from the shower axis the muons will be more dispersed in time than at smaller distances, leading to the dependence of the risetime on distance found experimentally (Fig. 2).

Because the muons are relatively energetic, the effects of velocity difference, of deflections in the geomagnetic field and of Coulomb scattering, are small, although these factors were taken into account even in the earliest Monte Carlo studies of the phenomenon [16]. By contrast, the electrons and photons of an air shower have mean energies of about 10 MeV so that the arrival of the electromagnetic component of the shower is delayed with respect to the muons because of the multiple scattering of the electrons. The delay of the electromagnetic component with respect to the muons also increases with distance.

The risetime is found experimentally to be a function of distance, zenith angle, and energy (Fig. 2). At 1000 m from the shower axis, for a vertical event of 10 EeV, $t_{1/2} \sim 380$ ns. This value increases slowly with energy and decreases with zenith angle. At large angles and/or small distances, $t_{1/2}$ can be comparable to the 25 ns resolution of the FADCs, and this fact restricts the data that are used below. The fastest risetime, measured in very inclined showers or with single muons, is 40 ns and is an indication of the limitations set by the

measurement technique and hence guides our selection of distance and angular ranges.

Because of the size of the Auger Observatory and the large separation of the detectors, it is necessary to take account of the fact that a detector that is struck early in the passage of the shower across the array will have a slower risetime than one that is struck later, even if the two detectors are at the same axial distance from the shower core. This asymmetry arises from a complex combination of attenuation of the electromagnetic component as the shower develops and because of the different part of the angular distribution of muons (more strictly of the parent pions) that is sampled at different positions across the array. The attenuation of the electromagnetic component of a shower across an array was first discussed by Greisen [17]. A detailed description of the asymmetry that is observed, and of its power for testing hadronic interaction models, has been given recently [6]. For the present study, the asymmetry is taken into account by referencing each risetime to that which would be recorded at a hypothetical detector situated at 90° with respect to the direction of the shower axis projected onto the ground, and at the same axial distance from the shower core, as the station at which a measurement is made. The amplitude of the asymmetry is a function of zenith angle, axial distance, and energy; at 40° , 750 m, and 10 EeV, it is $\sim 15\%$.

The magnitudes of the risetimes that are measured in a particular shower depend upon the development of the shower. As the energy increases, the mean position of the point of maximum development of the shower moves deeper into the atmosphere, and thus the risetimes will,

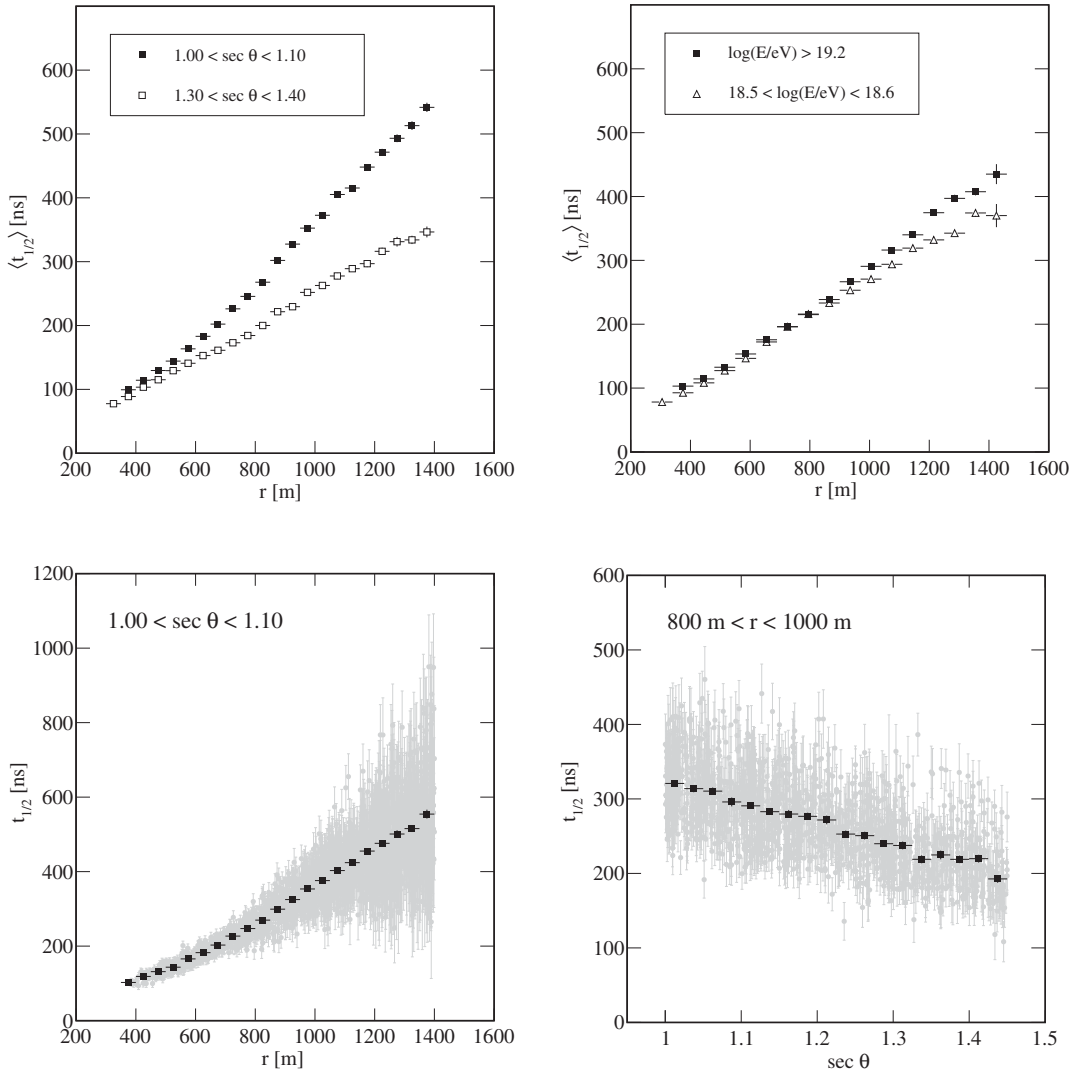


FIG. 2. (Top left) The risetime as a function of distance to the shower core for two different intervals of $\sec\theta$ in the energy range $19.0 < \log(E/eV) < 19.2$. (Top right) The risetime as a function of distance for two different energy bands in the angular range $1.20 < \sec\theta < 1.30$. (Bottom left) Illustration of the spread in the risetimes as a function of distance for events in the energy range $19.1 < \log(E/eV) < 19.2$. (Bottom right) Illustration of the variation of rise the time with a zenith angle for events in the energy range $19.1 < \log(E/eV) < 19.2$. All plots are based on experimental data.

on average, be slower than for a lower-energy event. Because muons dominate the shower to an increasing extent at large zenith angles, because the electromagnetic component suffers increased attenuation, the risetimes are expected to be faster at a detector that is at the same distance from the axis of the shower but in the vertical direction. The magnitude of the energy, distance, and zenith angle effects that can be inferred qualitatively from Fig. 1 are evident in the data shown in Fig. 2.

From these considerations, it follows that studying the risetimes of showers provides a method of measuring the shower development and thus of deducing the mass composition. Details of the study are presented below, where the risetime properties are also compared with predictions from Monte Carlo calculations using different hadronic models.

B. Determination of the accuracy of measurements of $t_{1/2}$

The uncertainty in a measurement of $t_{1/2}$ is found empirically from the data and will be described in some detail as it plays an essential role in the determination of the new parameter, introduced in Sec. IV, used to characterize shower development. The uncertainty can be obtained by using sets of detectors placed 11 m apart (known as “twins”) and also by using detectors that lie at similar distances from the shower core (“pairs”). Measurements made using twins and pairs cover different distance ranges. With twins, we can parametrize the uncertainty with a sufficient number of events only between 300 and 1200 m from the shower core. With pairs, we can cover distances from 600 to 1800 m. It is then natural to combine both sets of measurements to avoid

TABLE I. Selection of twin detectors used to assess the risetime uncertainty.

Cuts	750 m array		1500 m array	
	Number of twins	Efficiency	Number of twins	Efficiency
Pretwin selection	41,100	1.00	41,934	1.00
$5 < S/\text{VEM} < 800$	34,461	0.84	35,704	0.85
$r < 2000$ m	34,459	0.83	35,620	0.84
$ S_i - S_{\text{mean}} < 0.25S_{\text{mean}}$	28,466	0.69	29,832	0.71

as much as possible relying on extrapolations when estimating the uncertainty in the measurement of $t_{1/2}$.

The twin detectors give two independent measurements of the risetime at what is effectively a single point in the shower plane. Differences in the values of $t_{1/2}$ at the twins arise from the limitations set by the sampling of the shower front by a detector of finite size (10 m²) and from the measurement uncertainties intrinsic to the FADC system. For the more numerous pairs, there are the additional complications that arise from the asymmetry effect and from the difference in distance of the pairs from the shower core.

1. Assessment of measurement uncertainty using twin detectors

In the surface-detector array, there are 14 sets of twins and seven sets of triplets (three detectors on a triangular grid each separated by 11 m); the triplets are also referred to as twins. We parametrize the uncertainty by splitting the data in different bins of distance to the core, zenith angle, and detector signal. This implies that a precise parametrization of the uncertainty demands a large amount of data. To cope with this requirement, we must combine all twin

measurements that belong to events reconstructed at either of the arrays. A total of $\sim 83,000$ twin measurements are available from the two arrays for zenith angles below 60° and above energies of 0.3 and 1 EeV for events that trigger the two arrays. The cuts on energy and zenith angle are very loose to enhance the number of events available for analysis. Likewise, the criteria applied at detector level and detailed in Table I are mild to keep the selection efficiency as high as possible. We discard detectors that recorded a small number of particles or were located far from the core to avoid biases in the signal measurement. For very large signals, the risetime measurements approach the instrumental resolution and therefore are discarded. The cut on $|S_i - S_{\text{mean}}|$ in Table I is made to deal with cases in which one signal is typically around 5 VEM and the other, possibly because of an upward fluctuation, is relatively large. Such twins are rejected.

The average uncertainty in a risetime measurement, $\sigma_{1/2}$, is given by

$$\sigma_{1/2} = \frac{\sqrt{\pi}}{2} \langle |t_{1/2}^1 - t_{1/2}^2| \rangle, \quad (1)$$

where the superscripts define each member of the twin. As twin detectors are only 11 m apart, no correction is necessary for the azimuthal asymmetry.

The data have been divided into seven bins of width 0.1 in $\sec \theta$ and six distance ranges (see Fig. 3, left). The mean values of $\sigma_{1/2}$ as a function of signal size, S , are fitted with the function

$$\sigma_{1/2} = \sqrt{\left(\frac{J(r, \theta)}{\sqrt{S}}\right)^2 + \left(\sqrt{2} \frac{25 \text{ ns}}{\sqrt{12}}\right)^2}. \quad (2)$$

The first term in this function represents the differences seen between the two detectors, while the second term

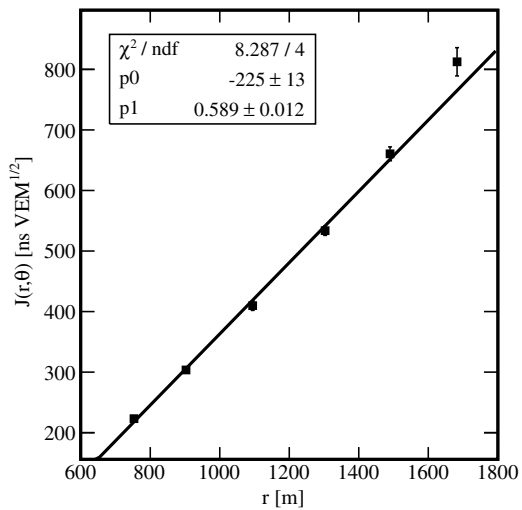
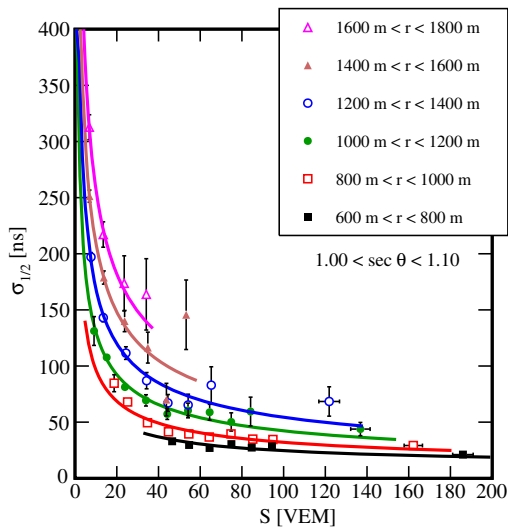


FIG. 3. (Left) Uncertainty obtained with pair detectors as a function of the station signal for vertical events ($1.00 < \sec \theta < 1.10$). Each line is the result of the fits performed for different distance ranges. Each point represents the average measurements of at least ten pair detectors. (Right) The parameter $J(r, \theta)$ as a function of the distance to the core for the same zenith angle range.

arises from the digitization of the signal in time intervals of 25 ns.

J is found from a linear function, $J(r, \theta) = p_0(\theta) + p_1(\theta) r$, and the fitted values of p_0 and p_1 as functions of $\sec \theta$ are

$$\begin{aligned} p_0(\theta) &= (-340 \pm 30) + (186 \pm 20) \sec \theta \\ p_1(\theta) &= (0.94 \pm 0.03) + (-0.44 \pm 0.01) \sec \theta, \end{aligned} \quad (3)$$

where p_0 units are (ns VEM^{1/2}) and p_1 units are (ns VEM^{1/2} m⁻¹).

2. Assessment of measurement uncertainty using pairs of detectors

For the purposes of this study, a pair of detectors is defined as any two detectors in the same shower in which the difference in the distance from the shower core ($|r_2 - r_1|$) is less than 100 m, irrespective of the azimuth angle. After applying the cuts previously discussed, there are $\sim 50\%$ more pair measurements than there are measurements from twins. This sample is large enough to allow us to limit this study to pairs of detectors from the 1500 m array only. However, corrections have to be made for the asymmetry, and because of the array spacing, there are no data below 600 m. Additionally, a correction must be made because the risetimes are at different axial distances; for a 100 m separation, this difference is ~ 30 ns, assuming a linear dependence of risetime with distance (see Fig. 2). Before applying this correction, the mean time difference for pairs was (14.750 ± 0.002) ns; after correction, the average difference was (0.140 ± 0.002) ns.

From an analysis similar to that described for the twin detectors, the fits for p_0 and p_1 have the parametrizations

$$\begin{aligned} p_0(\theta) &= (-447 \pm 30) + (224 \pm 20) \sec \theta \\ p_1(\theta) &= (1.12 \pm 0.03) + (-0.51 \pm 0.02) \sec \theta. \end{aligned} \quad (4)$$

The variation of J with distance is also shown in Fig. 3.

The differences in the values of p_0 and p_1 from the two analyses arise because they cover different distance ranges and different energy ranges. To optimize the determination of $\sigma_{1/2}$ for the risetimes measured at each station, we adopt the following parametrizations for p_0 and p_1 for different core ranges:

$$\begin{aligned} p_0(\theta) &= \begin{cases} (-340 \pm 30) + (186 \pm 20) \sec \theta & \text{if } r \leq 650 \text{ m} \\ (-447 \pm 30) + (224 \pm 20) \sec \theta & \text{if } r > 650 \text{ m} \end{cases} \\ p_1(\theta) &= \begin{cases} (0.94 \pm 0.03) + (-0.44 \pm 0.01) \sec \theta & \text{if } r \leq 650 \text{ m} \\ (1.12 \pm 0.03) + (-0.51 \pm 0.02) \sec \theta & \text{if } r > 650 \text{ m} \end{cases}. \end{aligned} \quad (5)$$

We have set the break point at 650 m because at this distance the uncertainties given by the two parametrizations agree within their statistical uncertainties (2–3 ns).

IV. NEW PARAMETER Δ_s AND ITS DETERMINATION FOR INDIVIDUAL AIR SHOWERS

A. Introduction to the Delta method

When a large number of risetimes is recorded in an event, it is possible to characterize that event by a single time just as the size of an event is designated by $S(1000)$, the signal size at 1000 m from the shower axis. This approach is only practical at high energies, as several measurements are needed to estimate the risetime at 1000 m by extrapolation [18]. Here, to obtain a large sample of data over a wide range of energies, an alternative method of using risetime measurements is introduced. We have determined for the two arrays independent relationships that describe the risetimes as a function of distance in a narrow range of energy (see Sec. IV. C). We call these functions ‘‘benchmarks,’’ and risetimes at particular stations, after correction for the asymmetry effect, are compared with the relevant times from the benchmark, $t_{1/2}^{\text{bench}}$, in units of the accuracy with which they are determined. The approach is illustrated in Fig. 4; the benchmarks are, of course, zenith-angle dependent (see Fig. 2). We use the term ‘‘Delta method’’ to refer to this approach in what follows.

Thus, for each measurement of $t_{1/2}$ at a single detector, i , an estimate of $\Delta_i = (t_{1/2} - t_{1/2}^{\text{bench}})/\sigma_{1/2}$ is made. Each shower is then characterized by Δ_s , the average of these estimates for the N selected stations,

$$\Delta_s = \frac{1}{N} \sum_{\text{stations}} \Delta_i. \quad (6)$$

B. Data selection

The data from the water-Cherenkov arrays were collected between January 1, 2004 (2008 for the 750 m spacing) and December 31, 2014. The first selection, of 6T5 events, has already been discussed. Other selections for the two arrays are shown in Table II.

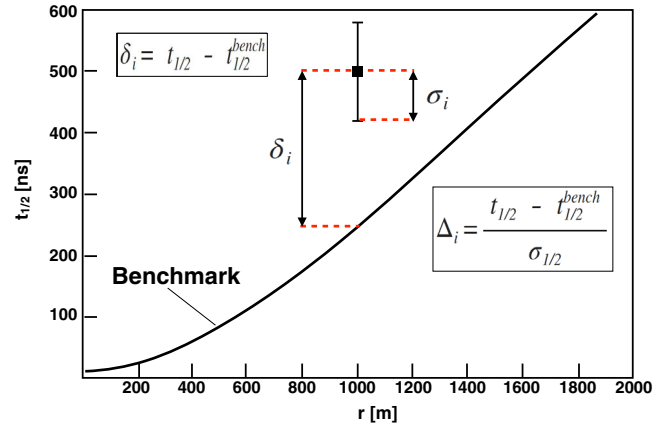


FIG. 4. Schematic diagram to illustrate the Delta method.

TABLE II. Quality cuts applied to the events of the 750 and 1500 m arrays. ϵ stands for the overall efficiency. The explanation for the different cuts can be found in the text.

750 m array			1500 m array		
Quality cuts	Events	ϵ (%)	Quality cuts	Events	ϵ (%)
$17.5 < \log(E/\text{eV}) < 18.5$	159,795	100.0	$\log(E/\text{eV}) > 18.5$	217,469	100.0
$\sec \theta < 1.30$	72,907	45.6	$\sec \theta < 1.45$	97,981	45.0
6T5 trigger	29,848	18.7	6T5 trigger	67,764	31.0
Reject bad periods	28,773	18.0	Reject bad periods	63,856	29.0
≥ 3 selected stations	27,553	17.2	≥ 3 selected stations	54,022	24.8

The lower-energy cuts are made to select events that trigger the arrays with 100% efficiency. The upper energy cut in the 750 m array is made to set aside events in overlapping energy regions that will be used later to cross-check the robustness of the method. As previously discussed, at large angles $t_{1/2}$ can be comparable to the 25 ns resolution of the FADCs, and this fact restricts the usable angular range. The cut in zenith angle is lower for the 750 m array than for the 1500 m array because the stations tend to be closer to the core and the limitations set by the sampling speed of the FADCs become more important at larger angles and small distances. We rejected data-taking periods in which the performance of the array of surface detectors is not optimal. At least three selected stations are required for an event to be included in the data samples.

The stations used within each event must fulfil the following criteria. The stations cannot be saturated in the low-gain channel since risetimes cannot be obtained from such signals. The signals recorded by the stations must be bigger than 3 VEM and 5 VEM for the 750 and 1500 m arrays, respectively. Those cuts guarantee that no bias toward primaries of a particular type is introduced; the difference in selection efficiency for protons and iron is less than 5% for all energy bins. The selected stations must lie within a given distance range from the position of the reconstructed core of the shower. The lower range of distance, 300 m, is selected to avoid the problems set by the inability of the recording system to record fast pulses (see Sec. III.A), while the upper ranges [800 m (1400 m) for the 750 m (1500 m) array] are chosen to span what is consistent with unbiased selection. For the highest energies, this has been extended to 2000 m as the signal sizes in such events are sufficiently large to give accurate measurements. For the 750 and 1500 m arrays, the overall selection efficiencies at station level are 52% and 56%, respectively. This translates into 113,661 and 210,709 detectors for the 750 and 1500 m arrays, respectively.

Using simulations, we have searched for biases that might be introduced into inferences about mass composition as a result of these cuts. The difference between the overall selection efficiencies for protons and Fe nuclei are smaller than 2%. The upper limit on the energy cut in the 750 m data eliminates only 2% of the events. This cut, and

the lower-energy limit for the 1500 m array, are relaxed later to study the overlap region in detail.

For the 750 and 1500 m arrays, the mean numbers of selected stations per event satisfying the selection criteria defined in Table II are 4.0 and 3.6, respectively. In the analysis discussed below, selected events are required to have three or more values of Δ_r , but for an arrival direction study, in which it is desirable to separate light from heavy primaries, one could envisage using two stations, or even one, to infer the state of development of the shower, albeit with more limited accuracy.

C. Determination of the benchmarks for the 750 and 1500 m arrays

The determination of the benchmarks, which define the average behavior of the risetimes as a function of distance and zenith angle, is fundamental to the success of the technique. Essentially the same procedures have been adopted for both arrays. For each detector, two time traces are recorded on high-gain and low-gain channels. The risetime of a detector is computed according to the following procedure: in the case in which no saturation occurs, the risetime is obtained from the trace corresponding to the high-gain channel. If this channel is saturated, we use the trace from the low-gain channel to compute the risetime. If the low-gain signal is saturated as well, which can occur for stations close to the core in high-energy events, that station is not selected for this analysis. Further details of the recording procedures are given in Ref. [8].

In computing the benchmarks, account must be taken of the fact that the risetimes measured for a station in the two channels are not identical, as illustrated in Fig. 5. During the digitization process, a threshold that removes very small signals is imposed. The net effect of this threshold affects the low-gain traces much more, since their signals are smaller due to the lower signal-to-noise ratio when compared to the one associated to high-gain traces. The influence of tails in the determination of the integrated signal is therefore reduced for low-gain signals, and as a consequence, the risetime measurement is affected. This instrumental effect makes it necessary to obtain benchmarks for the high-gain and the low-gain traces independently.

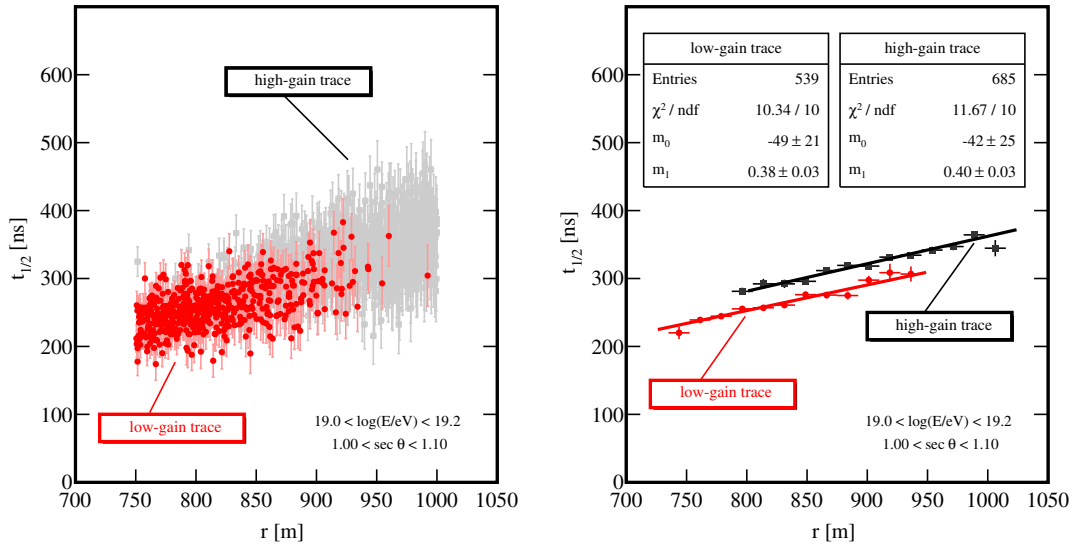


FIG. 5. (Left) Risetimes as a function of core distance for events with and without saturation in the high-gain channel. We have selected events with energies $19.0 < \log(E/eV) < 19.2$ and zenith angles $1.00 < \sec \theta < 1.10$. (Right) Same as the left plot, but this time, we show average values to make more evident the difference between measurements when the saturation of the high-gain channel is present.

As shown in Table II, the energy ranges covered by the two arrays are $17.5 < \log(E/eV) < 18.5$ (750 m spacing) and $\log(E/eV) > 18.5$ (1500 m spacing). The energy bins chosen for the benchmarks of the 750 and 1500 m arrays are $17.7 < \log(E/eV) < 17.8$ and $19.1 < \log(E/eV) < 19.2$, respectively. The choices for the benchmarks are most effective in dealing with the high-gain/low-gain problem just discussed. They guarantee that we reject a reduced number of detectors in which the low- and the high-gain channels are simultaneously saturated and therefore allow a definition of the benchmark over a broad distance range. In addition, this implies that the distance intervals used to fit the behavior of the risetimes computed either with the low- or the high-gain traces are sufficiently long to avoid compromising the quality of the fit.

A fit is first made to the data from the low-gain channels using the relation

$$t_{1/2}^{\text{low-gain trace}} = 40 \text{ ns} + \sqrt{A(\theta)^2 + B(\theta)r^2} - A(\theta), \quad (7)$$

where A and B are free parameters. The reason for adopting 40 ns as a limit was explained in Sec. III.A. Other functions were tested; this one gave consistently lower values of reduced χ^2 over the range of angles and energies used for the two arrays.

Having used low-gain traces to evaluate A and B , the signals from high-gain traces are now fitted with the function

$$t_{1/2}^{\text{high-gain trace}} = 40 \text{ ns} + N(\theta) \left(\sqrt{A(\theta)^2 + B(\theta)r^2} - A(\theta) \right), \quad (8)$$

in which there is one free parameter, $N(\theta)$, that describes the shift between the measurements in the two channels. Examples of the quality of the fits of these functions to the data are shown in Figs. 6 and 7 for two angular ranges for each of the two arrays.

In the right-hand plots of each pair, the mean and rms deviations of the fits are seen to be consistent with 0 and 1, as expected for pull distributions [19]. The uncertainty in the axial distance has not been included in the fits as it is only around 2% for the distances in question.

Fits were made for A , B , and $N(\theta)$ in six intervals of $\sec \theta$ ranges 1.0–1.30 and 1.0–1.45 for the 750 and 1500 m arrays, respectively. In all six cases, the χ^2 values of the fits are between 1 and 1.2. To obtain the final parametrization of A , B , and N as a function of θ , fits have been made using the functions

$$\begin{aligned} A(\theta) &= a_0 + a_1(\sec \theta)^{-4} \\ B(\theta) &= b_0 + b_1(\sec \theta)^{-4} \\ N(\theta) &= n_0 + n_1(\sec \theta)^2 + n_2 e^{\sec \theta}, \end{aligned} \quad (9)$$

where the seven coefficients, a_0 , a_1 , etc., are determined for the two arrays. This set of functions has been empirically chosen. It guarantees that, for the energy bins for which the benchmarks are defined, the mean value of Δ_s shows a flat behavior as a function of $\sec \theta$. This naturally follows from the definition of $t_{1/2}^{\text{bench}}$. Since it embodies the dependence on $\sec \theta$, the numerator in the definition of Δ_i has to be independent of the zenith angle.

We may thus define the benchmarks in terms of A , B , and N as a function of $\sec \theta$, enabling an appropriate

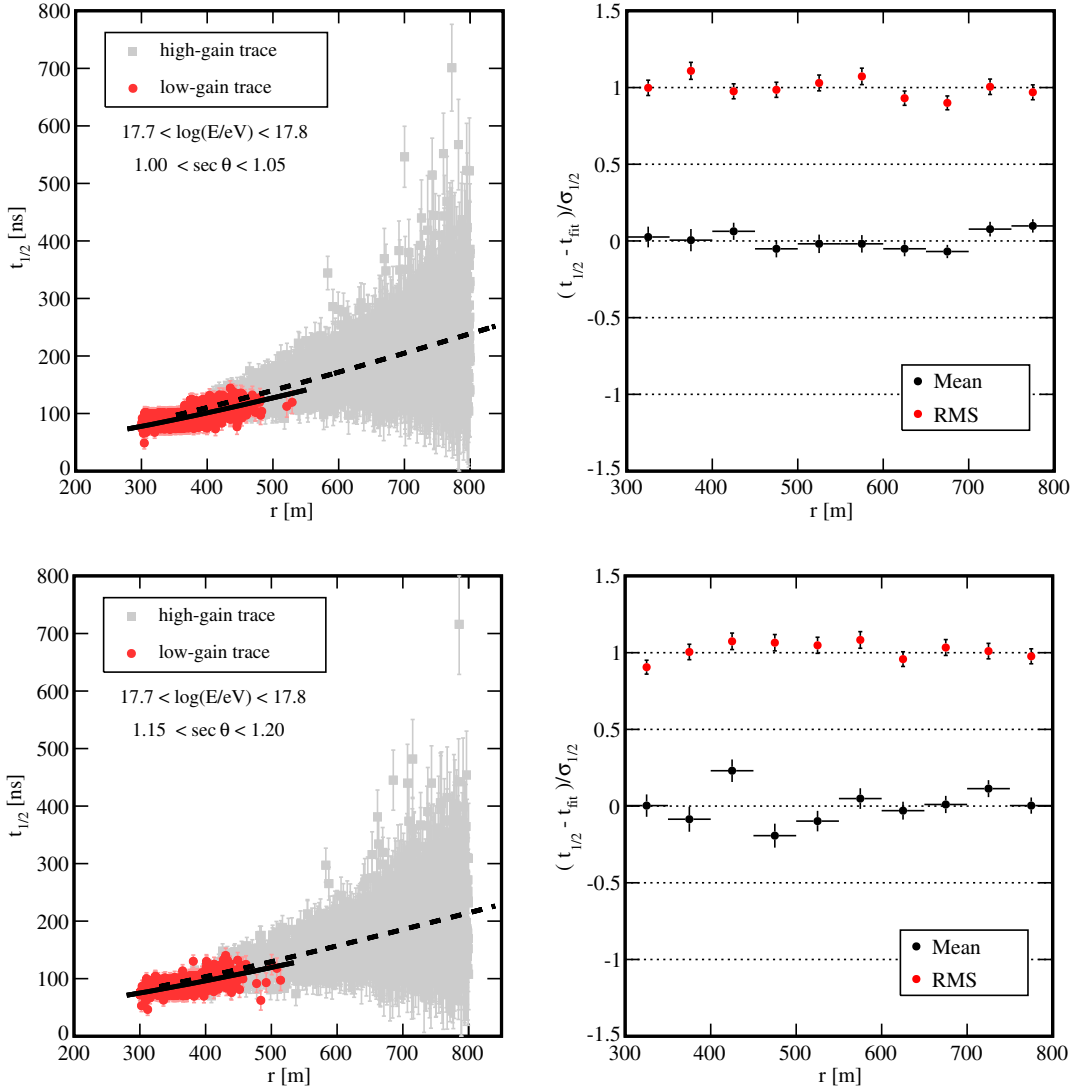


FIG. 6. Examples of benchmark fit for the 750 m array. (Top panels) $1.00 < \sec \theta < 1.05$. (Bottom panels) $1.15 < \sec \theta < 1.20$. The solid (dashed) line corresponds to the fit done to the risetimes computed using the low-gain (high-gain) trace.

benchmark to be defined for the zenith angle of the event under study. Thus, Δ_i can be found for every station that satisfies the selection criterion, and the corresponding value of Δ_s can be found for every selected event.

V. EVOLUTION OF $\langle \Delta_s \rangle$ WITH ENERGY AND COMPARISON WITH MODEL PREDICTIONS

We now describe the observed variation of $\langle \Delta_s \rangle$, the mean of Δ_s for a set of events, as a function of energy. The selection criteria for this analysis were presented in Table II. The variation of $\langle \Delta_s \rangle$ with energy for the two arrays is shown in Fig. 8. Note that at the benchmark energies, indicated by the vertical bands, $\langle \Delta_s \rangle$ is zero, as expected by definition.

The results shown in Fig. 8 were obtained using the whole data set. We produce similar plots, but this time split data in different bands of $\sec \theta$. This exercise gives results

that are consistent with the ones displayed in Fig. 8. Searches for anomalous behavior of the largest, the second-largest, and the smallest signals separately have also been made; none was found.

To test the validity of hadronic models, we can use $\langle \Delta_s \rangle$. In previous works [4–7], strong evidence has been found that the models do not adequately describe the data and that the problem lies with the predictions of the muon content of showers. As the risetime is dominated by muons, $\langle \Delta_s \rangle$ is expected to provide further investigation of this problem that will be useful because of the higher number of events and the extension to lower energies.

Libraries of simulations for the QGSJetII-04 [20] and EPOS-LHC [21] models and proton and iron primaries for zenith angles $< 45^\circ$ and $17.5 < \log(E/eV) < 20$ have been created. In making comparisons with data, it is necessary to choose which benchmarks to adopt. For consistency in

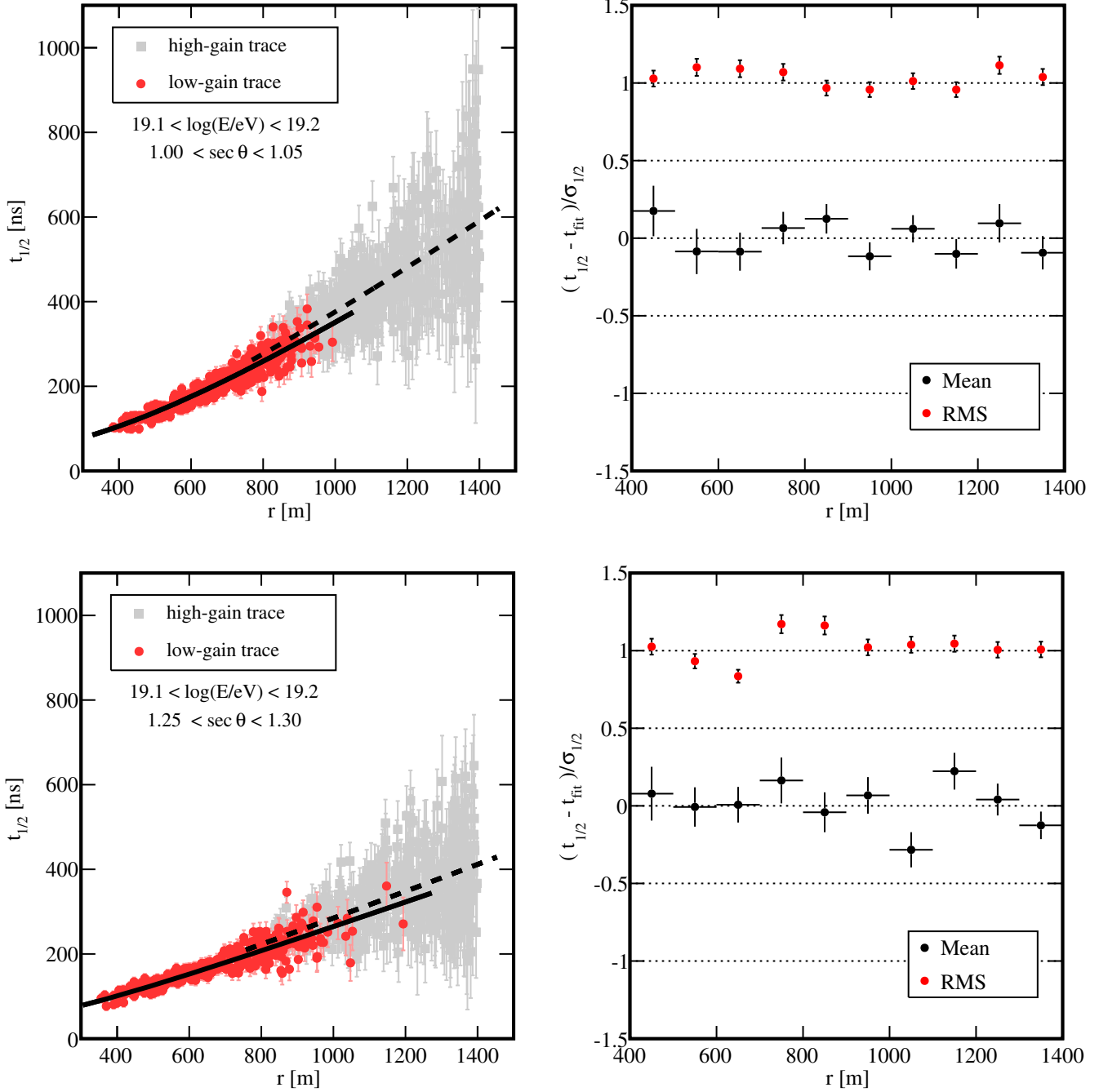


FIG. 7. Examples of benchmark fit for the 1500 m array. (Top panels) $1.00 < \sec \theta < 1.05$. (Bottom panels) $1.25 < \sec \theta < 1.30$. The solid (dashed) line corresponds to the fit done to the risetimes computed using the low-gain (high-gain) trace.

what follows, we use the benchmarks determined from data (Sec. IV). Different choices of benchmarks would simply give shifts in the values of $\langle \Delta_s \rangle$, which would be the same for each data set.

For this study, the uncertainties in the risetimes have been found from simulations and adopting the twins approach described in Sec. III. The results are shown in Fig. 9, in which it is seen that the uncertainties from the data are in good agreement with simulations using the QGSJetII-04 model at the benchmark energy.

A comparison of the evolution of $\langle \Delta_s \rangle$ with energy from the data with those from models is shown in Fig. 10 (see Tables VI and VII).

The main sources that contribute to the systematic uncertainty are a seasonal effect found when data are grouped according to the season of the year. It amounts to 0.03 for the 1500 m data, and it is due to the variable conditions of pressure and temperature found in the atmosphere through the year. The UTC time at which the data were recorded also introduces a small uncertainty

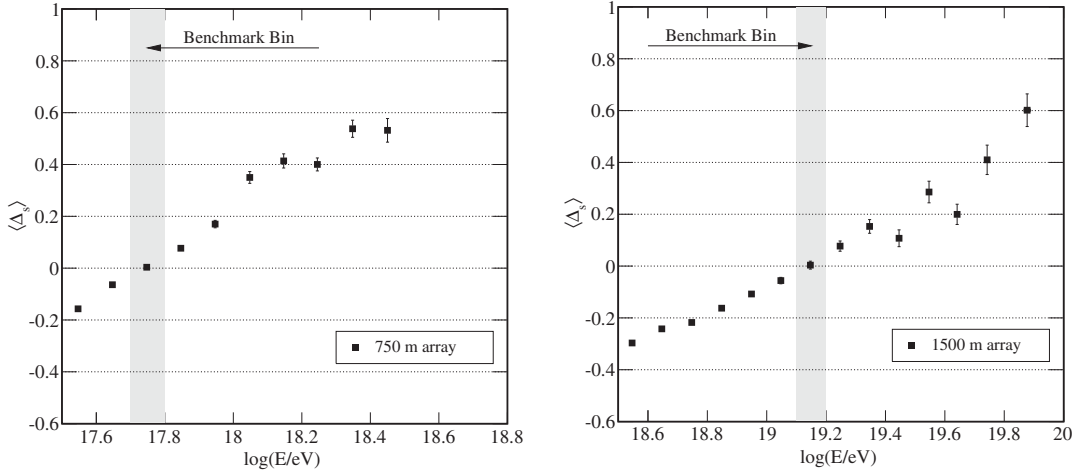


FIG. 8. Evolution of $\langle \Delta_s \rangle$ as a function of energy for the two surface arrays: 750 m (left) and 1500 m (right). The gray bands show the energy ranges in which the benchmark functions were defined.

in our determination of $\langle \Delta_s \rangle$. Splitting data into periods corresponding to day and night, we obtain a value of this uncertainty of 0.01 for the 1500 m array data. Our observable also exhibits dependence with the aging effects of surface detectors. We take as a systematic uncertainty the difference in $\langle \Delta_s \rangle$ found after grouping our data into two samples, one running from 2004 to 2010 and the other one from the years 2012 to 2014. For the 1500 m array, the difference amounts to 0.04. A small dependence of $\langle \Delta_s \rangle$

with $\sec \theta$ is taken as source of systematics, its value being 0.02. Finally, the systematic uncertainty associated to the energy scale ($\pm 14\%$) results in a systematic uncertainty on $\langle \Delta_s \rangle$ that amounts to 0.1. Adding all these contributions in quadrature, the overall systematic uncertainty in $\langle \Delta_s \rangle$ is 0.11 for the 1500 m array. A similar study for the 750 m array gives an overall systematic uncertainty in $\langle \Delta_s \rangle$ of 0.07. According to simulations, this is about 10% of the separation between proton and iron nuclei. It is evident, independent of which model is adopted, that the measurements suggest an increase of the mean mass with energy above ~ 2.5 EeV if the hadronic models are correct.

Assuming the superposition model is valid and since $\langle \Delta_s \rangle$ is proportional to the logarithm of the energy (Fig. 8), the mean value of the natural logarithm of A (the atomic weight of an element) can be found from the following equation:

$$\langle \ln A \rangle = \ln 56 \frac{\langle \Delta_s \rangle_p - \langle \Delta_s \rangle_{\text{data}}}{\langle \Delta_s \rangle_p - \langle \Delta_s \rangle_{\text{Fe}}}. \quad (10)$$

The results of this transformation for two models are shown in Fig. 11 and are compared with the Auger measurements of X_{max} made with the FD [22]. While the absolute values of $\langle \ln A \rangle$ for the Delta method and the FD X_{max} differ from each other, the trend in $\langle \ln A \rangle$ with energy is very similar. The observed difference arises because of the inadequate description of the muon component in the models used to get the $\langle \ln A \rangle$ values. Notice that the electromagnetic cascade dominates the FD measurement, whereas the Delta method is of a parameter that is a mixture of muons and the electromagnetic component. With substantially more events than in previous studies, we observe that the inconsistency between data and model predictions extends over a greater energy range than what was probed in past works.

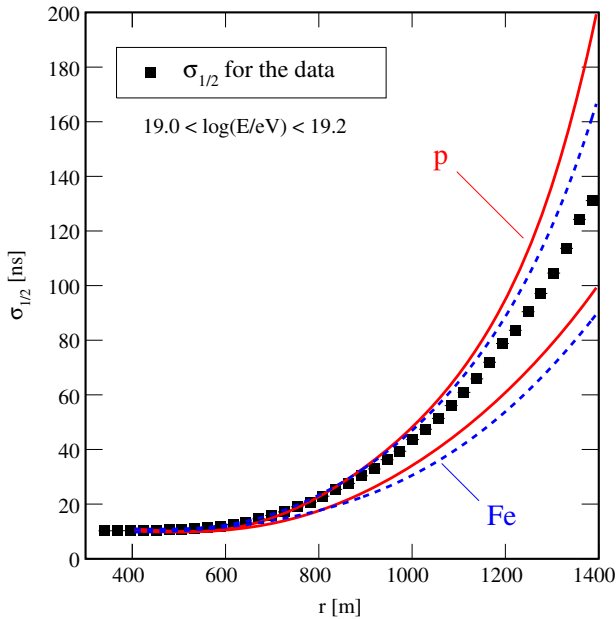


FIG. 9. Risettime uncertainties estimated for protons (red lines), iron nuclei (blue dashed lines), and data as a function of core distance. For a clear view, the uncertainties corresponding to data are the average values. The uncertainties have been evaluated for events with energies in the range $19.0 < \log(E/eV) < 19.2$. The regions bracketed by the lines indicate the spread of the events simulated with QGSJetII-04 at a given distance.

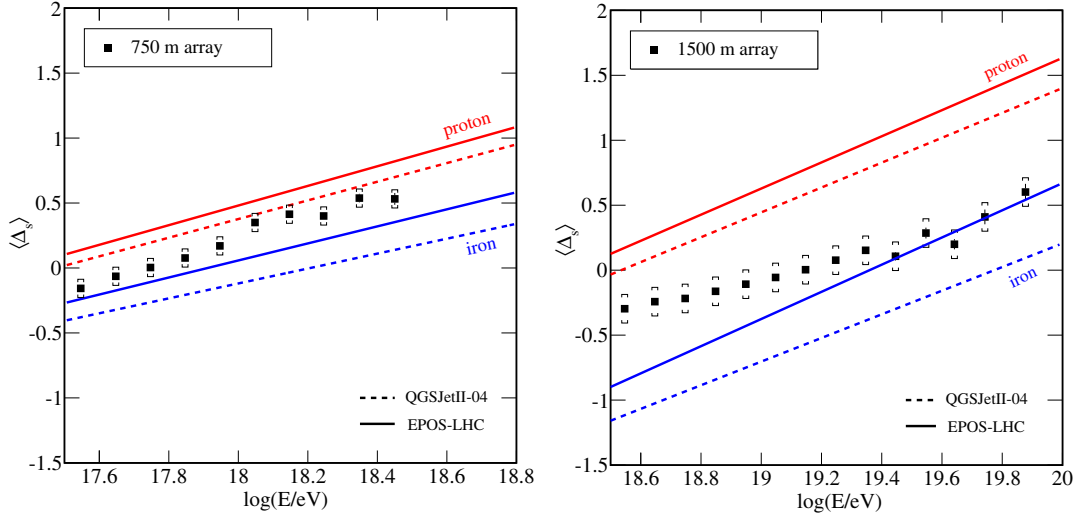


FIG. 10. $\langle \Delta_s \rangle$ as a function of the energy for the two surface arrays. Brackets correspond to the systematic uncertainties. Data are compared to the predictions obtained from simulations.

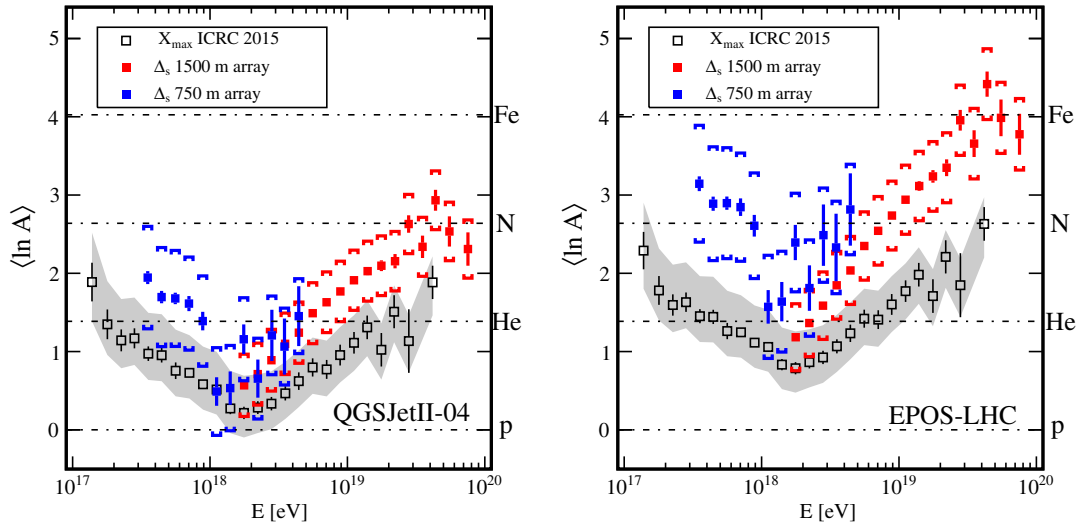


FIG. 11. $\langle \ln A \rangle$ as a function of energy for the Delta method and for X_{\max} measurements done with the FD. QGSJetII-04 and EPOS-LHC have been used as the reference hadronic models. Statistical uncertainties are shown as bars. Brackets and shaded areas correspond to the systematic uncertainties associated to the measurements done with the SD and FD data, respectively.

In Fig. 12, the Delta results are also compared with the results of the analysis made using the asymmetry method [6] and with those from the study of the depth of muon production [4].

For EPOS-LHC, the results from the asymmetry analysis, which is also based on risetimes and consequently on signals that are a mixture of the muon and the electromagnetic component, are in good agreement with the Delta results, albeit within the rather large statistical uncertainties. By contrast, the results from the muon production depth analysis, in which only muons are studied, give much larger (and astrophysically unexpected) values of $\langle \ln A \rangle$. This once more indicates that the mechanisms of muon production in extensive air showers are not properly described in current hadronic models.

VI. CORRELATION OF Δ_s WITH THE DEPTH OF SHOWER MAXIMUM

We now address the correlation of Δ_s with the depth of shower maximum, X_{\max} . As remarked earlier, we would not expect a 1:1 correlation between these parameters because the muon/electromagnetic mix incident on the water-Cherenkov detectors changes in a complex, but well-understood, manner with zenith angle, energy, and distance. An idea of the correlation to be expected can be gained through Monte Carlo studies.

Values of Δ_s and X_{\max} have been obtained from simulations of 1000 proton and 1000 iron nuclei showers made using the QGSJetII-04 model for the benchmark bin of the 1500 m array. The results are shown for three stations

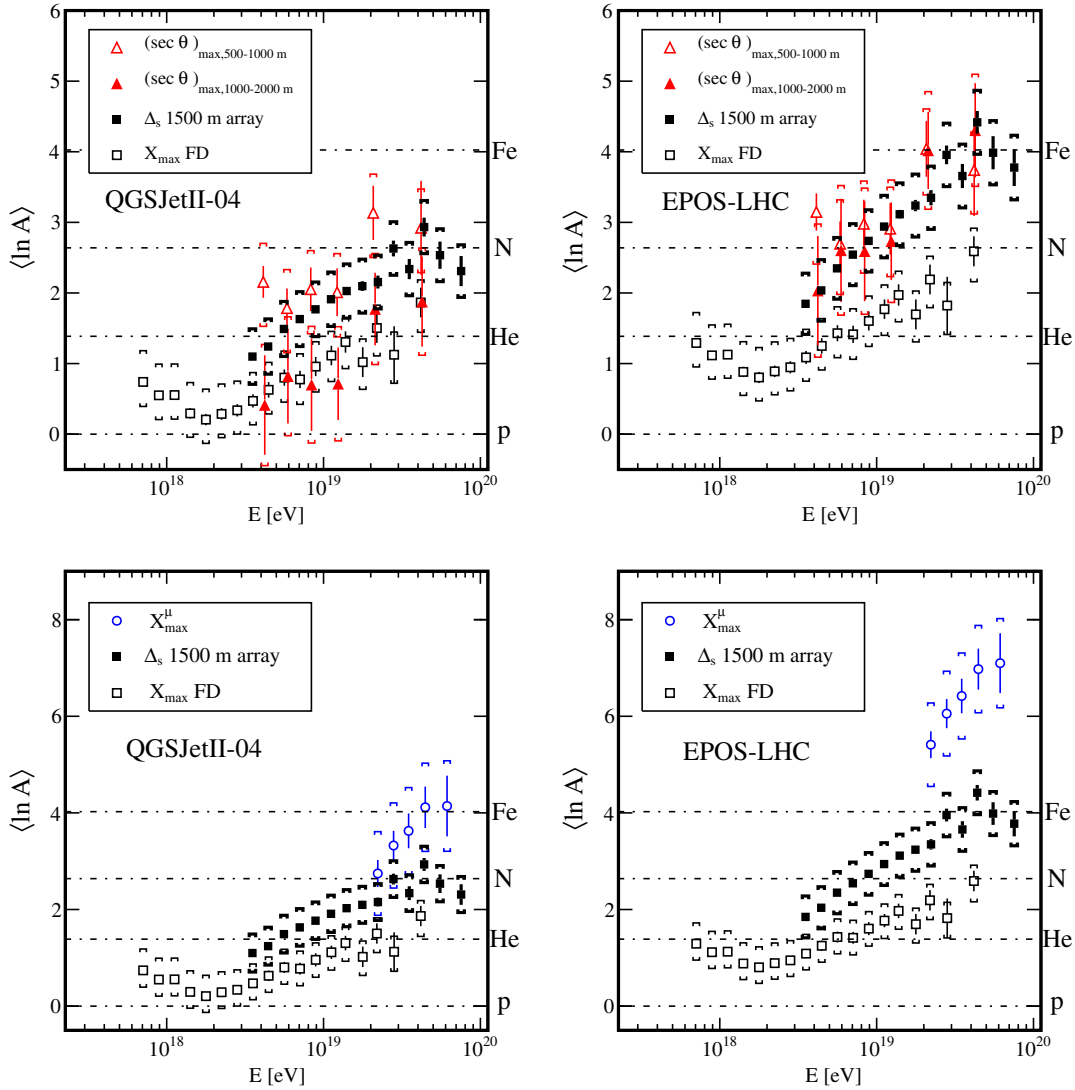


FIG. 12. $\langle \ln A \rangle$ as a function of the energy for analyses using FD data and SD data from the 1500 m array. QGSJetII-04 and EPOS-LHC have been used as the reference hadronic models. The results of the Delta method are compared with those arising from the asymmetry analysis [6] (top panels) and from the Muon Production Depth analysis [4] (bottom panels). Brackets correspond to the systematic uncertainties.

in Fig. 13. The fact that the Pearson correlation is less strong for Fe nuclei than for protons reflects the enhanced dominance of muons in showers initiated by Fe primaries. The simulations give an indication of what is to be expected when the measurements of Δ_s are compared with the X_{\max} values in the hybrid events for which the reconstruction of both observables is possible.

To exploit the correlation using data, and hence extend the energy range and the statistical significance of the elongation rate determined with the FD, it is necessary to create empirical correlations using events in which both Δ_s and X_{\max} have been measured in the same events. For this study, we used the data discussed in Ref. [1] for the 1500 m array for the events with energies >3 EeV and a similar set of data from the 750 m array [22] for events of lower energy. The selection of events is shown in Table III.

The Δ_s and X_{\max} of the events selected for the purposes of calibration are shown for the two arrays in Fig. 14. There are 252 and 885 events for the 750 and 1500 m arrays, respectively, available for calibration of which 161 have energies >10 EeV. The small number for the 750 m array reflects the shorter period of operation and the relatively small area (23.5 km^2) of the array. We have checked that the sample of events selected is unbiased by comparing the elongation rate determined from the full data set (from HEAT and standard fluorescence telescopes) with that found from the 252 and 885 events alone.

For the calibration, we fit functions of the form

$$X_{\max} = a + b\Delta_s + c \log(E/\text{eV}) \quad (11)$$

to the two data sets. The term b is dominant in the fit. The term c is included to accommodate the energy dependence

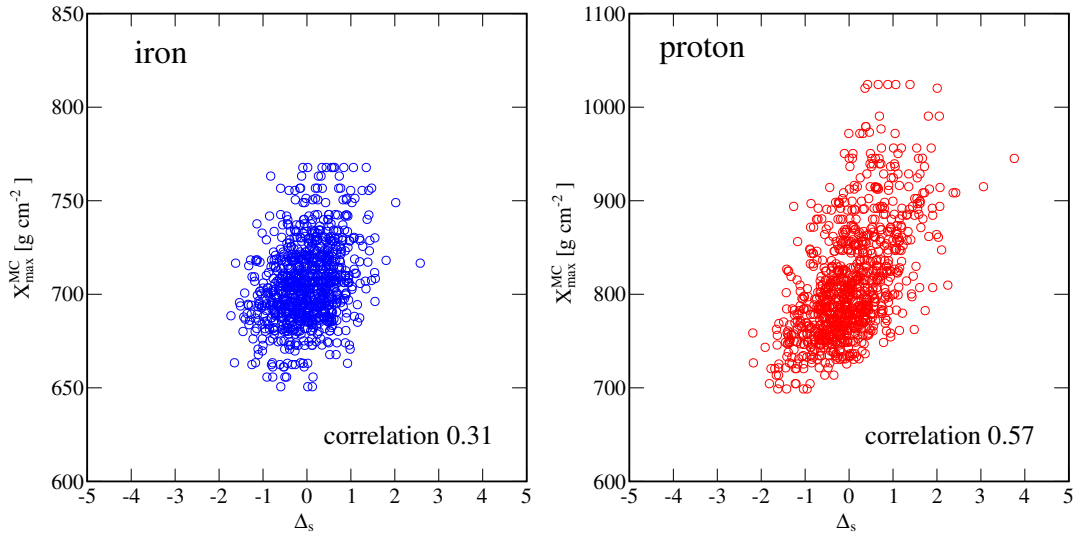


FIG. 13. Pearson's correlation of Δ_s and the true values of X_{\max} for events simulated with QGSJetII-04 in the energy range $19.1 < \log(E/\text{eV}) < 19.2$. The left panel corresponds to iron nuclei; the right panel shows the correlation for protons. Values of Δ_s are computed for three stations.

TABLE III. Set of cuts used to select events simultaneously reconstructed by the fluorescence and surface detectors. These events are used for calibration purposes. ϵ stands for the overall efficiency. HEAT data are obtained with a set of three fluorescence detectors that point to the higher zenith angles appropriate to the lower energies.

750 m array			1500 m array		
Quality cuts	Events	ϵ (%)	Quality cuts	Events	ϵ (%)
HEAT data	12,003	100.0	FD data	19,759	100.0
FD & SD reconstruction	2461	20.5	FD & SD reconstruction	12,825	65.0
$\sec \theta < 1.30$	2007	16.7	$\sec \theta < 1.45$	9625	49.0
6T5 trigger	714	5.9	6T5 trigger	7361	37.0
≥ 3 selected stations	660	5.5	≥ 3 selected stations	4025	20.0
$\log(E/\text{eV}) \geq 17.5$	252	2.1	$\log(E/\text{eV}) \geq 18.5$	885	4.5

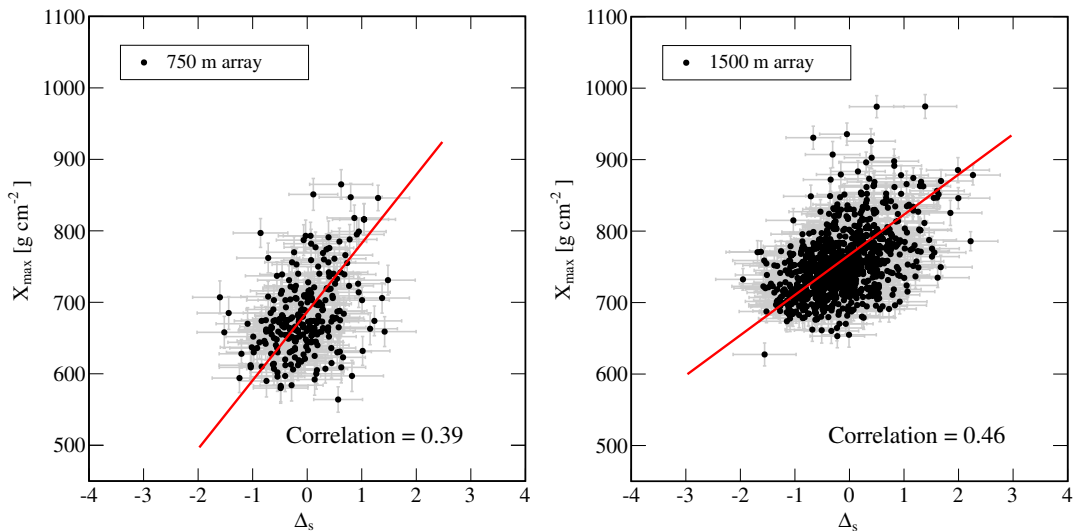


FIG. 14. (Left) Correlation of X_{\max} and Δ_s for the 252 events from the 750 m array. (Right) Correlation of X_{\max} and Δ_s for the 885 events of the 1500 m array.

TABLE IV. Coefficients obtained from the calibration of Δ_s and X_{\max} .

Calibration parameters	750 m array Value (g cm^{-2})	1500 m array Value (g cm^{-2})
a	636 ± 20	699 ± 12
b	96 ± 10	56 ± 3
c	2.9 ± 1.2	3.6 ± 0.7

of both variables. A fit including a quadratic term in $\log(E/\text{eV})$ does not modify our results. The uncertainties in X_{\max} are taken from Ref. [1]. We have used the maximum likelihood method to make the fits that give the coefficients listed in Table IV. The three coefficients are not independent. Their Pearson correlations are $\rho_{ab} = -0.2$, $\rho_{ac} = -0.97$, and $\rho_{bc} = 0.34$. These correlations are taken into account when evaluating the systematic uncertainty associated with the calibration procedure.

We have also evaluated the systematic uncertainties associated with the measurements of X_{\max} deduced from the surface detectors. These include the seasonal, diurnal, aging, and θ dependence already discussed for $\langle\Delta_s\rangle$ in Sec. V that X_{\max} propagate to our measurement. Now, two further sources of systematics arise. One is related to the uncertainty in the calibration parameters. We have propagated this uncertainty, taking into account the correlation of the parameters a , b , and c . For the 1500 m array, the differences in X_{\max} span from 3 g cm^{-2} at the lowest energies to 5 g cm^{-2} at the upper end of the energy spectrum. We quote conservatively as a systematic uncertainty the largest value found and consider it constant for the whole energy range. A similar procedure for the 750 m array data results in a systematic uncertainty of 10 g cm^{-2} . The systematic uncertainty obtained in the measurement of X_{\max} with the FD detector propagates directly into the values obtained with the SD data. In Ref. [1], the systematic uncertainty varies as a function of the energy. In this analysis, the average of those values is quoted a systematic

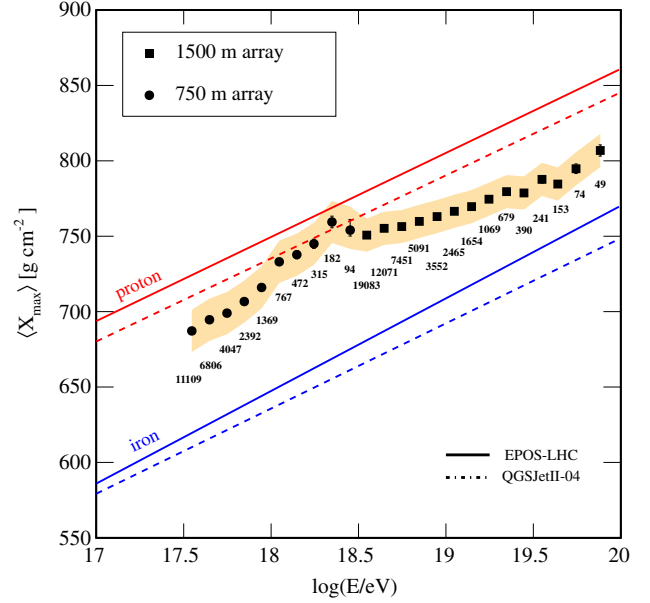


FIG. 15. Mean values of the X_{\max} distributions obtained with the data of the 750 and 1500 m surface arrays as a function of the energy. The shaded area indicates the systematic uncertainties. Data are compared to the predictions from simulations of protons and iron nuclei for two different hadronic models. The number of selected events in each energy bin is indicated.

uncertainty that is constant with energy. The values are shown for each effect and for each array in Table V.

The systematic uncertainties have been added in quadrature to give 14 and 11 g cm^{-2} for the 750 and 1500 m arrays, respectively.

The values of X_{\max} found from this analysis are shown as a function of energy in Fig. 15 (see Tables VIII and IX). The resolution in the measurement of X_{\max} with the surface-detector data is 45 g cm^{-2} .

In Fig. 16, measurements in the region of overlap between the two arrays are shown. The agreement is satisfactory.

TABLE V. Breakdown of the systematic uncertainties of X_{\max} for the 750 and 1500 m arrays. The systematic uncertainties in the measurements of X_{\max} with the FD and HEAT detectors propagate directly into the values obtained with the SD data. The rest of systematic uncertainties quoted in this table are intrinsic to the Delta method.

750 m array		1500 m array	
Source	Systematic uncertainty (g cm^{-2})	Source	Systematic uncertainty (g cm^{-2})
Uncertainty on calibration	10.0	Uncertainty on calibration	5.0
Seasonal effect	2.0	Seasonal effect	2.0
Diurnal dependence	1.0	Diurnal dependence	1.0
Aging	3.0	Aging	3.0
HEAT systematic uncertainty	8.5	FD systematic uncertainty	8.5
Angular dependence	<1.0	Angular dependence	1.5
Total	14.0	Total	11.0

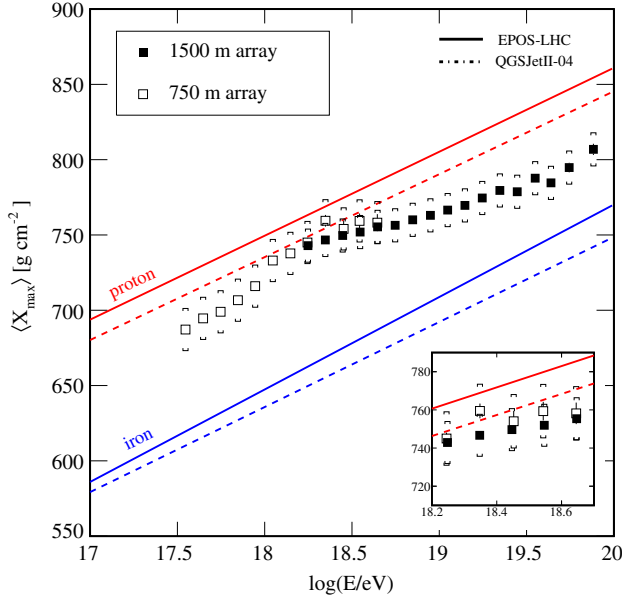


FIG. 16. Same as Fig. 15 including additional X_{\max} measurements from the surface detectors above and below 3 EeV. (Inset) Three energy bins have been included below 3 EeV using the data of the 1500 m array, and two measurements added above 3 EeV use the data of the 750 m array. There is good agreement between measurements in the overlap region. The brackets correspond to systematic uncertainties.

In Fig. 17, the data of Fig. 15 are compared with measurements made with the fluorescence detectors [22].

The agreement is good; the results from the surface detector alone are statistically stronger and extend to higher energies.

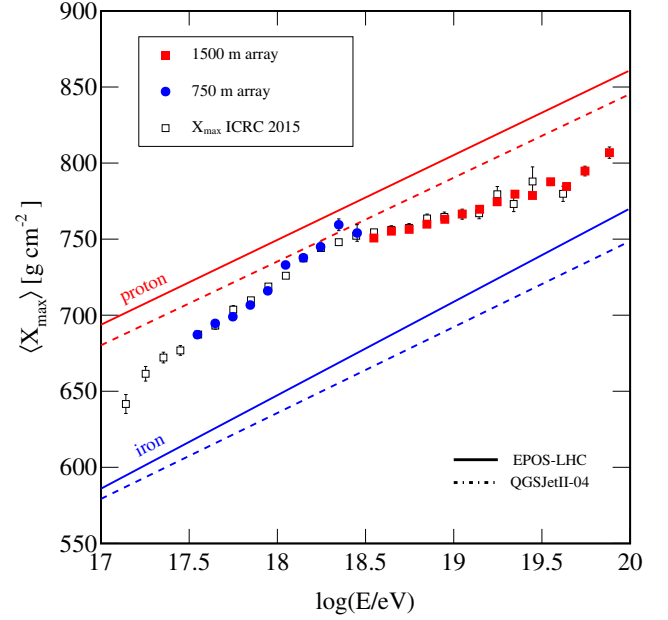


FIG. 17. Evolution of $\langle X_{\max} \rangle$ as a function of energy. The figure compares the mean values of the X_{\max} distributions measured by the fluorescence and surface detectors of the Pierre Auger Observatory. In most cases, the uncertainties are smaller than the size of the symbols.

A. Interpretation of the measurements in terms of average mass

A comparison with hadronic models allows the expression of the average depth of shower maxima in terms of the natural logarithm of the atomic mass $\langle \ln A \rangle$, following the procedure discussed in Sec. V. The evolution of $\langle \ln A \rangle$ as a function of energy is shown in Fig. 18. In the energy

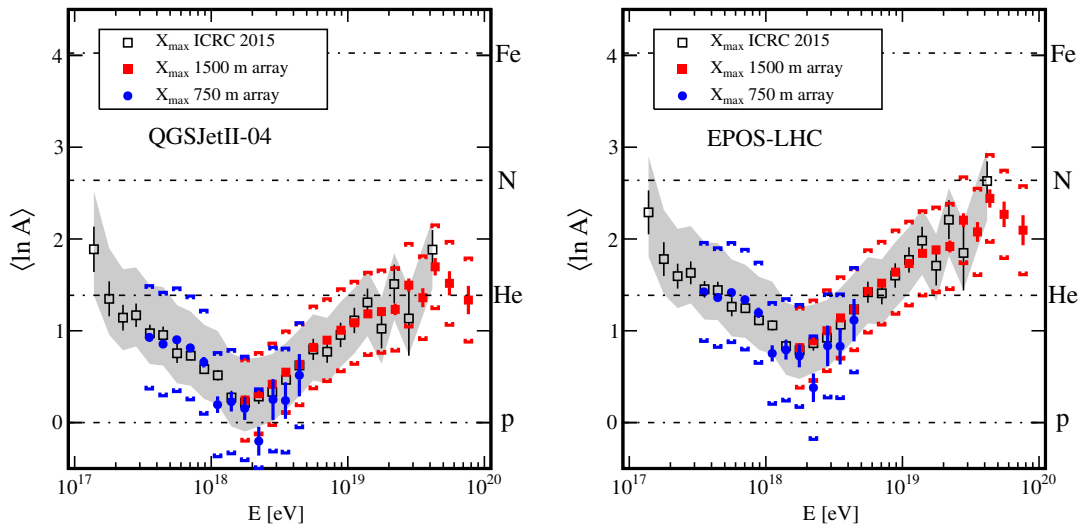


FIG. 18. $\langle \ln A \rangle$ as a function of the energy. QGSJetII-04 and EPOS-LHC have been used as the reference hadronic models. The results of the Delta method are compared with those based on X_{\max} measurements done with the FD [22]. Brackets and shaded areas correspond to the systematic uncertainties; bars correspond to uncertainties of statistical nature.

range in which the FD and SD measurements coincide, the agreement is good. For both hadronic models, the evolution of $\langle \ln A \rangle$ with energy is similar. However, the EPOS-LHC model suggests a heavier average composition. SD measurements have been used to confirm, with a larger data set, what has already been observed with FD measurements, namely, that the primary flux of particles is predominantly composed of light particles at around 2 EeV and that the average mass increases up to ~ 40 EeV. Above this energy, the SD measurements can be used to draw inferences about mass composition with good statistical power. The last two bins indicate a possible change in the dependence of X_{\max} with energy above 50 EeV, with the final point lying ~ 3 sigma above the elongation rate fitted to data above 3 EeV. It is, therefore, possible that the increase of the primary mass with energy is slowing at the highest energies, but we need to reduce statistical and systematic uncertainties further before strong conclusions can be drawn. AugerPrime, the upgrade of the surface-detector array of the Pierre Auger Observatory [23], will significantly improve our capability to elucidate mass composition on an event-by-event basis in the energy range of the flux suppression.

VII. SUMMARY AND CONCLUSIONS

We have described a new method for extracting relevant information from the time profiles of the signals from the water-Cherenkov detectors of the Pierre Auger Observatory. With it, we have been able to obtain information on the evolution of the mean depth of shower maximum with energy over a larger energy range than has been studied previously using over 81,000 events, of which 123 are of energy > 50 EeV. We have also been able to expand the discussions of the mismatch between data and predictions from models based on extrapolations of hadronic interactions from LHC energies. Specifically, we have reported the following:

- (1) The comparison of the risetime data with fluorescence measurements reinforces the conclusions reported previously [4–7] that the modeling of showers provides an inadequate description of air-shower data. The deductions are made over a larger energy range and with smaller statistical uncertainties than hitherto (Figs. 10 and 11).
- (2) The depth of shower maximum has been measured from 0.3 to 100 EeV using data of the surface detector (Fig. 15).
- (3) Data from the 750 m array of the Observatory have been used to derive mass information for the first time.

- (4) The mean measurements of X_{\max} have been compared with predictions from the EPOS-LHC and QGSJETII04 models and estimates of $\langle \ln A \rangle$ extracted (Fig. 18). While the EPOS-LHC model leads to larger values of $\langle \ln A \rangle$ than are found with the other model, both show the general trend of the mean mass becoming smaller as the energy increases up to ~ 2 EeV, after which it rises slowly with energy up to about 50 EeV where this rise seems to stop.

ACKNOWLEDGMENTS

The successful installation, commissioning, and operation of the Pierre Auger Observatory would not have been possible without the strong commitment and effort from the technical and administrative staff in Malargüe. We are very grateful to the following agencies and organizations for financial support: (Argentina) Comisión Nacional de Energía Atómica; Agencia Nacional de Promoción Científica y Tecnológica (ANPCyT); Consejo Nacional de Investigaciones Científicas y Técnicas (CONICET); Gobierno de la Provincia de Mendoza; Municipalidad de Malargüe; and NDM Holdings and Valle Las Leñas in gratitude for their continuing cooperation over land access; (Australia) the Australian Research Council; (Brazil) Conselho Nacional de Desenvolvimento Científico e Tecnológico (CNPq); Financiadora de Estudos e Projetos (FINEP); Fundação de Amparo à Pesquisa do Estado de Rio de Janeiro (FAPERJ); São Paulo Research Foundation (FAPESP) Grants No. 2010/07359-6 and No. 1999/05404-3; Ministério de Ciência e Tecnologia (MCT); (Czech Republic) Grants No. MSMT CR LG15014, LO1305, LM2015038, and CZ.02.1.01/0.0/0.0/16_013/0001402; (France) Centre de Calcul IN2P3/CNRS; Centre National de la Recherche Scientifique (CNRS); Conseil Régional Ile-de-France; Département Physique Nucléaire et Corpusculaire (PNC-IN2P3/CNRS); Département Sciences de l’Univers (SDU-INSU/CNRS); Institut Lagrange de Paris (ILP) Grant No. LABEX ANR-10-LABX-63 within the Investissements d’Avenir Programme Grant No. ANR-11-IDEX-0004-02; (Germany) Bundesministerium für Bildung und Forschung (BMBF); Deutsche Forschungsgemeinschaft (DFG); Finanzministerium Baden-Württemberg; Helmholtz Alliance for Astroparticle Physics (HAP); Helmholtz-Gemeinschaft Deutscher Forschungszentren (HGF); Ministerium für Innovation, Wissenschaft und Forschung des Landes Nordrhein-Westfalen; Ministerium für Wissenschaft, Forschung und Kunst des Landes Baden-Württemberg; (Italy) Istituto Nazionale di Fisica Nucleare (INFN); Istituto Nazionale di Astrofisica (INAF); Ministero dell’Istruzione, dell’Università e della Ricerca (MIUR); CETEMPS Center

of Excellence; Ministero degli Affari Esteri (MAE); (Mexico) Consejo Nacional de Ciencia y Tecnología (CONACYT) Grant No. 167733; Universidad Nacional Autónoma de México (UNAM); PAPIIT DGAPA-UNAM; (Netherlands) Ministerie van Onderwijs, Cultuur en Wetenschap; Nederlandse Organisatie voor Wetenschappelijk Onderzoek (NWO); Stichting voor Fundamenteel Onderzoek der Materie (FOM); (Poland) National Centre for Research and Development, Grants No. ERA-NET-ASPERA/01/11 and No. ERA-NET-ASPERA/02/11; National Science Centre, Grants No. 2013/08/M/ST9/00322, No. 2013/08/M/ST9/00728, No. HARMONIA 5–2013/10/M/ST9/00062, and No. UMO-2016/22/M/ST9/00198; (Portugal) Portuguese national funds and FEDER funds within Programa Operacional Factores de Competitividade through Fundação para a Ciência e a Tecnologia (COMPETE); (Romania) Romanian Authority for Scientific Research ANCS; CNDI-UEFISCDI partnership projects Grants No. 20/2012, No. 194/2012, and No. PN 16 42 01 02; (Slovenia) Slovenian Research Agency; (Spain) Comunidad de Madrid; Fondo Europeo de Desarrollo Regional (FEDER) funds; Ministerio de Economía y Competitividad; Xunta de Galicia; European Community 7th Framework Program Grant No. FP7-PEOPLE-2012-IEF-328826; (USA) Department of Energy, Contracts No. DE-AC02-07CH11359, No. DE-FR02-04ER41300, No. DE-FG02-99ER41107, and No. DE-SC0011689; National Science Foundation, Grant No. 0450696; The Grainger Foundation; Marie Curie-IRSES/EPLANET (European Union); European Particle Physics Latin American Network; European Union 7th Framework Program, Grant No. PIRSES-2009-GA-246806; European Union’s Horizon 2020 Research and Innovation Programme (Grant No. 646623); and UNESCO.

APPENDIX: DATA TABLES

TABLE VI. Values of $\langle\Delta_s\rangle$ for the 750 m array. The fourth column shows the statistical uncertainty. For all measurements, the systematic uncertainty amounts to 0.07.

Log (E/eV) range	$\langle\text{Log}(E/eV)\rangle$	$\langle\Delta_s\rangle$	$\sigma_{\text{stat}}(\langle\Delta_s\rangle)$
[17.5,17.6)	17.55	-0.157	0.009
[17.6,17.7)	17.65	-0.064	0.009
[17.7,17.8)	17.75	0.004	0.008
[17.8,17.9)	17.85	0.077	0.011
[17.9,18.0)	17.95	0.170	0.014
[18.0,18.1)	18.05	0.35	0.02
[18.1,18.2)	18.15	0.41	0.03
[18.2,18.3)	18.25	0.40	0.03
[18.3,18.4)	18.35	0.54	0.03
[18.4,18.5)	18.45	0.53	0.05

TABLE VII. Values of $\langle\Delta_s\rangle$ for the 1500 m array. The fourth column shows the statistical uncertainty. For all measurements, the systematic uncertainty amounts to 0.11.

Log (E/eV) range	$\langle\text{Log}(E/eV)\rangle$	$\langle\Delta_s\rangle$	$\sigma_{\text{stat}}(\langle\Delta_s\rangle)$
[18.5,18.6)	18.55	-0.297	0.005
[18.6,18.7)	18.65	-0.242	0.006
[18.7,18.8)	18.75	-0.218	0.007
[18.8,18.9)	18.85	-0.163	0.009
[18.9,19.0)	18.95	-0.108	0.011
[19.0,19.1)	19.05	-0.056	0.012
[19.1,19.2)	19.15	0.004	0.015
[19.2,19.3)	19.25	0.077	0.020
[19.3,19.4)	19.35	0.15	0.03
[19.4,19.5)	19.45	0.11	0.03
[19.5,19.6)	19.55	0.29	0.04
[19.6,19.7)	19.64	0.20	0.04
[19.7,19.8)	19.74	0.41	0.06
[19.8, ∞)	19.88	0.60	0.06

TABLE VIII. Values of $\langle X_{\text{max}}\rangle$ for the 750 m array. The fourth column shows the statistical uncertainty. For all measurements, the systematic uncertainty amounts to 14 g cm^{-2} .

Log (E/eV) range	$\langle\text{Log}(E/eV)\rangle$	$\langle X_{\text{max}}/\text{g cm}^{-2}\rangle$	$\sigma_{\text{stat}}(\langle X_{\text{max}}\rangle)/\text{g cm}^{-2}$
[17.5,17.6)	17.55	687.2	0.5
[17.6,17.7)	17.65	695.6	0.6
[17.7,17.8)	17.75	699.9	0.8
[17.8,17.9)	17.85	707	1.0
[17.9,18.0)	17.95	716	1.0
[18.0,18.1)	18.05	733	2.0
[18.1,18.2)	18.15	738	3.0
[18.2,18.3)	18.25	745	3.0
[18.3,18.4)	18.35	759	4.0
[18.4,18.5)	18.45	754	5.0

TABLE IX. Values of $\langle X_{\text{max}}\rangle$ for the 1500 m array. The fourth column shows the statistical uncertainty. For all measurements, the systematic uncertainty amounts to 11 g cm^{-2} .

Log (E/eV) range	$\langle\text{Log}(E/eV)\rangle$	$\langle X_{\text{max}}/\text{g cm}^{-2}\rangle$	$\sigma_{\text{stat}}(\langle X_{\text{max}}\rangle)/\text{g cm}^{-2}$
[18.5,18.6)	18.55	750.7	0.3
[18.6,18.7)	18.65	755.2	0.3
[18.7,18.8)	18.75	756.4	0.4
[18.8,18.9)	18.85	759.8	0.6
[18.9,19.0)	18.95	763.0	0.6
[19.0,19.1)	19.05	766.5	0.7
[19.1,19.2)	19.15	769.6	0.9
[19.2,19.3)	19.25	775	1.0
[19.3,19.4)	19.35	780	2.0
[19.4,19.5)	19.45	779	2.0
[19.5,19.6)	19.55	788	2.0
[19.6,19.7)	19.64	785	2.0
[19.7,19.8)	19.74	795	3.0
[19.8, ∞)	19.88	807	3.0

- [1] A. Aab *et al.* (Pierre Auger Collaboration), *Phys. Rev. D* **90**, 122005 (2014).
- [2] R. U. Abbasi *et al.*, *Astropart. Phys.* **64**, 49 (2015).
- [3] A. Aab *et al.* (Pierre Auger Collaboration), *Phys. Rev. D* **90**, 122006 (2014).
- [4] A. Aab *et al.* (Pierre Auger Collaboration), *Phys. Rev. D* **90**, 012012(2014); **90**, 039904(A)(2014); **92**, 019903(E)(2015).
- [5] A. Aab *et al.* (Pierre Auger Collaboration), *Phys. Rev. D* **91**, 032003 (2015); **91**, 059901(E) (2015).
- [6] A. Aab *et al.* (Pierre Auger Collaboration), *Phys. Rev. D* **93**, 072006 (2016).
- [7] A. Aab *et al.* (Pierre Auger Collaboration), *Phys. Rev. Lett.* **117**, 192001 (2016).
- [8] A. Aab *et al.* (Pierre Auger Collaboration), *Nucl. Instrum. Methods Phys. Res., Sect. A* **798**, 172 (2015).
- [9] X. Bertou *et al.* (Pierre Auger Collaboration), *Nucl. Instrum. Methods Phys. Res., Sect. A* **568**, 839 (2006).
- [10] J. Abraham *et al.* (Pierre Auger Collaboration), *Nucl. Instrum. Methods Phys. Res., Sect. A* **613**, 29 (2010).
- [11] D. Newton, J. Knapp, and A. A. Watson, *Astropart. Phys.* **26**, 414 (2007).
- [12] J. Abraham *et al.* (Pierre Auger Collaboration), *Phys. Rev. Lett.* **101**, 061101 (2008).
- [13] V. Verzi, *Proc. Sci.*, ICRC2015 (2016) 015.
- [14] A. A. Watson and J. G. Wilson, *J. Phys. A* **7**, 1199 (1974).
- [15] J. Linsley and L. Scarsi, *Phys. Rev.* **128**, 2384 (1962).
- [16] A. J. Baxter, *J. Phys. A: Math. Gen.* **2**, 50 (1968).
- [17] K. Greisen, *Annu. Rev. Nucl. Part. Sci.* **10**, 63 (1960).
- [18] Pierre Auger Collaboration (to be published).
- [19] L. Demotier and L. Lyons, Report No. CDF/ANAL/PUBLIC/5776, 2002.
- [20] S. Ostapchenko, *Phys. Rev. D* **83**, 014018 (2011).
- [21] T. Pierog, I. Karpenko, J. M. Katzy, E. Yatsenko, and K. Werner, *Phys. Rev. C* **92**, 034906 (2015).
- [22] A. Porcelli (Pierre Auger Collaboration), *Proc. Sci.*, ICRC2015 (2016) 420.
- [23] A. Aab *et al.* (Pierre Auger Collaboration), *arXiv*: 1604.03637.